

Resuspension of Flooded Mine Tailings

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The UNIVERSITY of WESTERN ONTARIO

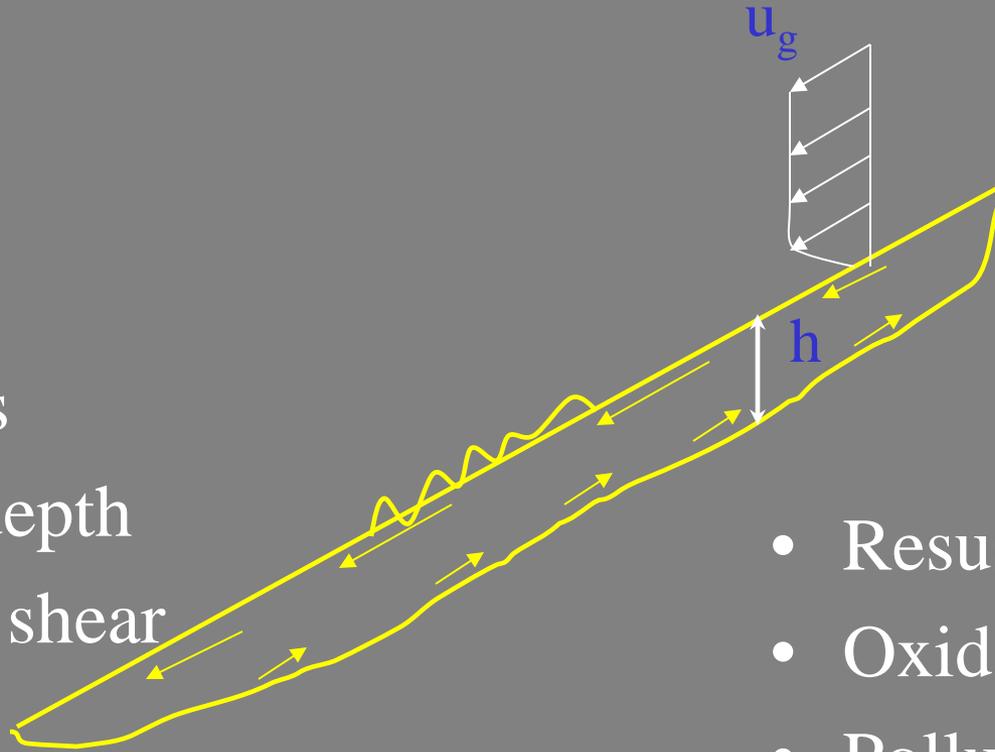
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- 5 Research Collaborators (Profs at Western)

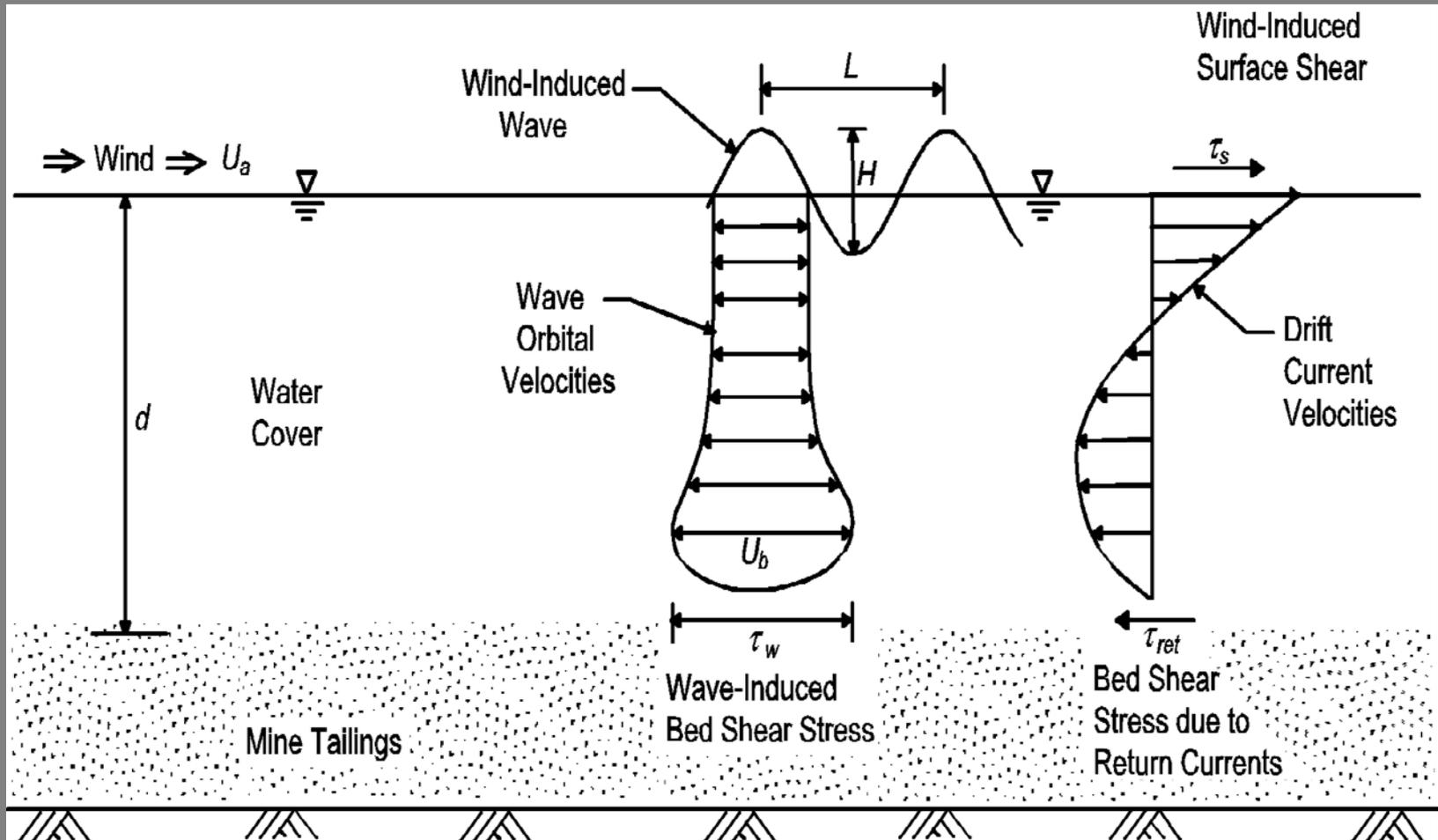
Water cover

- Wind
- Current
- Waves
- Tailings
- Water depth
- Critical shear stress



- Resuspension
- Oxidation
- Pollution

Schematic of Conceptual Tailings Pond Hydrodynamics

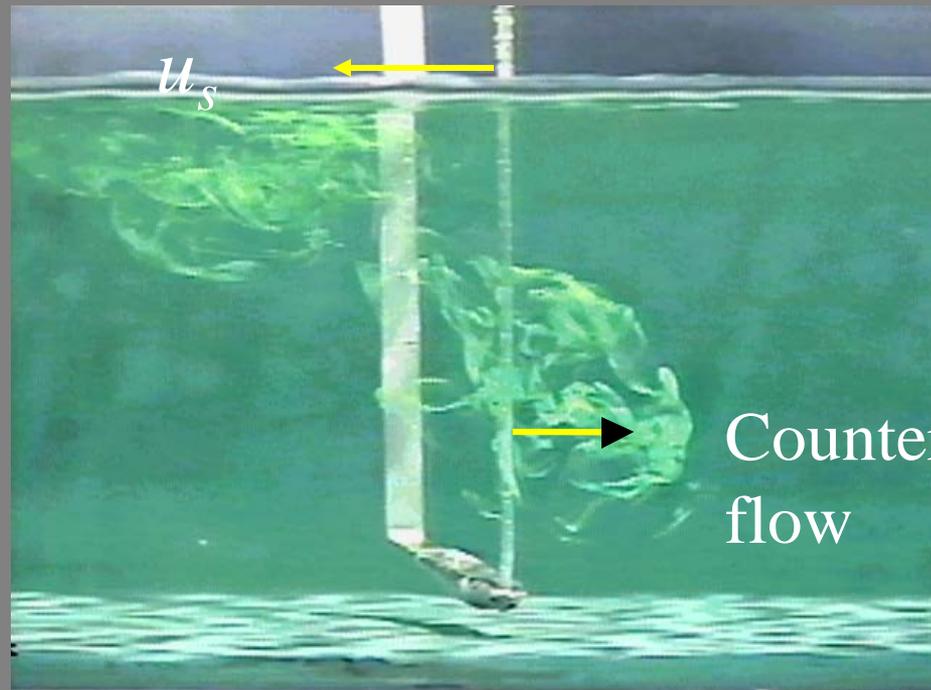


Flow field visualization

for wind speed $u_g=6.39\text{m/s}$ and water depth $h=63.5\text{ mm}$
(Deep water wave)

← **Wind**

Surface drift



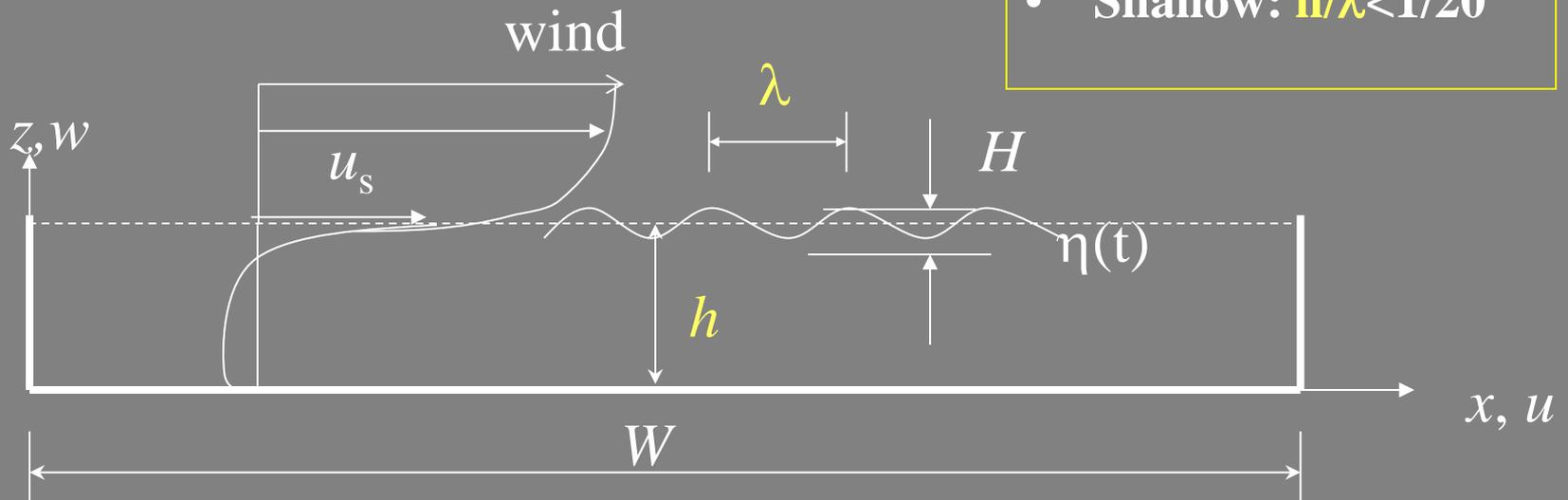
Countercurrent
flow

Study of surface **shear** and **waves** induced countercurrent flow

- Experimental Study
- Mathematical modeling

Classification of waves

- Deep: $h/\lambda > 1/2$
- Intermediate: $1/20 < h/\lambda < 1/2$
- Shallow: $h/\lambda < 1/20$



Field Resuspension Studies

- Field Studies
 - Heath Steele Upper and Lower Cells near Miramichi, New Brunswick
 - Quirke Cell 14, near Elliot Lake, Ontario
 - Falconbridge New Tailings Area, Near Sudbury, Ontario
- Laboratory Studies
 - Wave Tank and Wind-Wave Tank Experiments



Heath Steele

QUEBEC

QUEBEC

MAINE

UNITED STATES

PRINCE EDWARD ISLAND

NOVA SCOTIA

Gulf of St. Lawrence

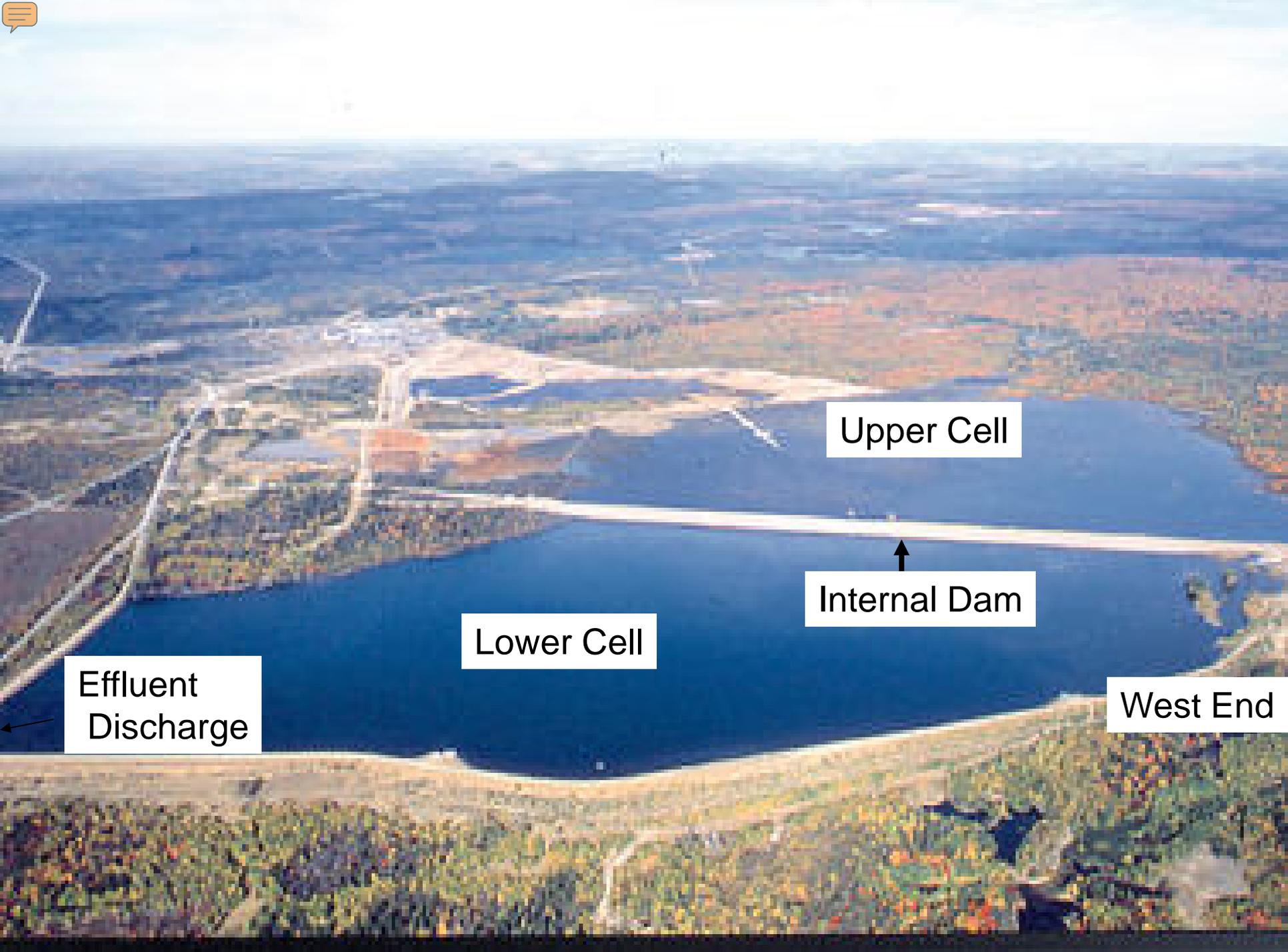
Bay of Fundy

Confederation Bridge

NEW BRUNSWICK

- CITIES**
- ★ Political subdivision capitals
 - Cities
- BOUNDARIES**
- International
 - Political subdivision





Upper Cell

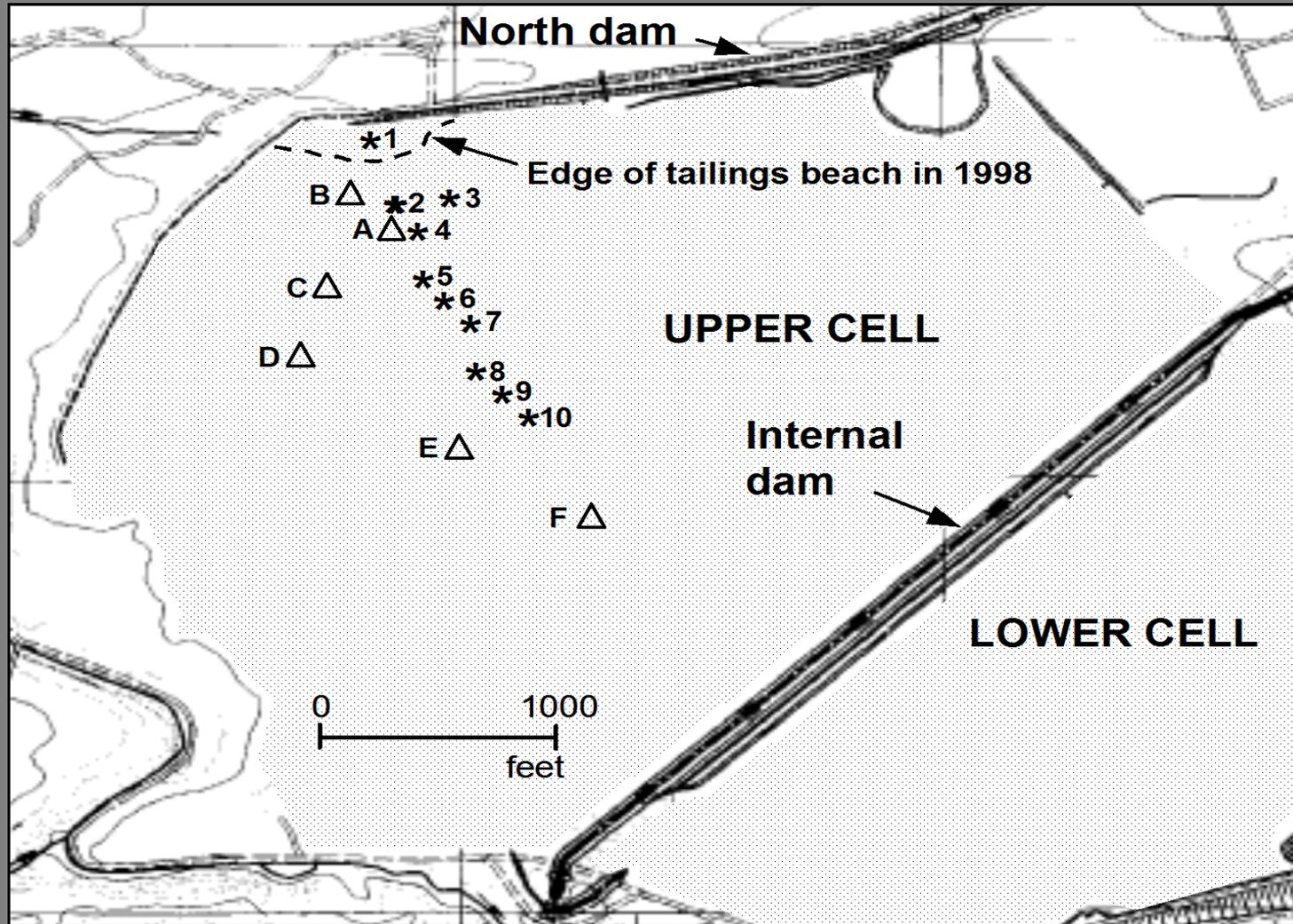
↑
Internal Dam

Lower Cell

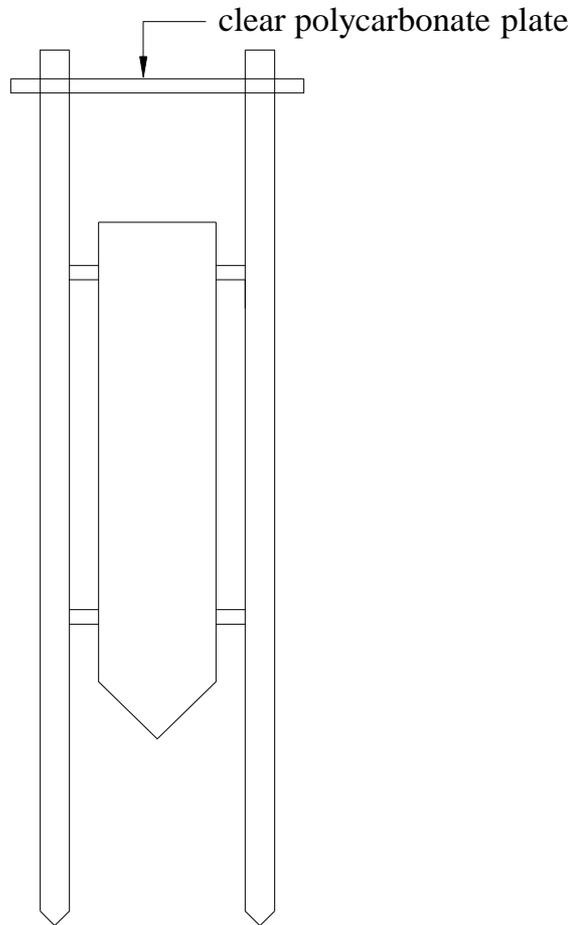
←
Effluent Discharge

West End

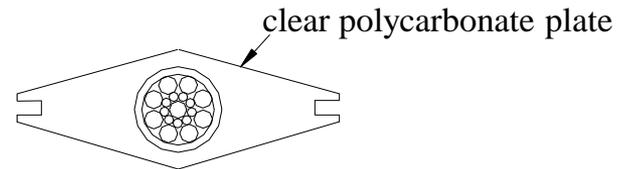
Heath Steele Upper Cell Tailings Pond Showing Sediment Trap Locations



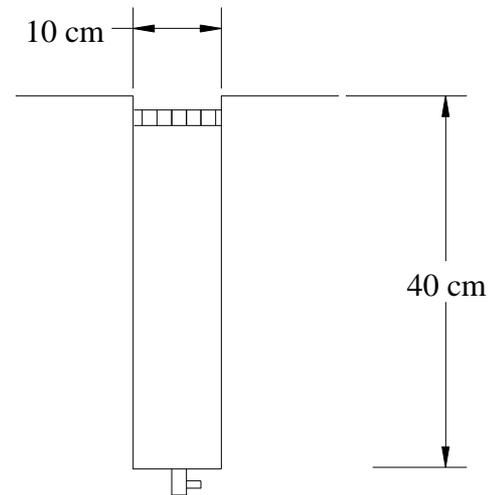
Schematic of sediment trap



Stainless steel container to hold trap in place



Plan view of sediment trap



Side view of sediment trap





Wind Measurements

- Wind Speed
- Wind Direction

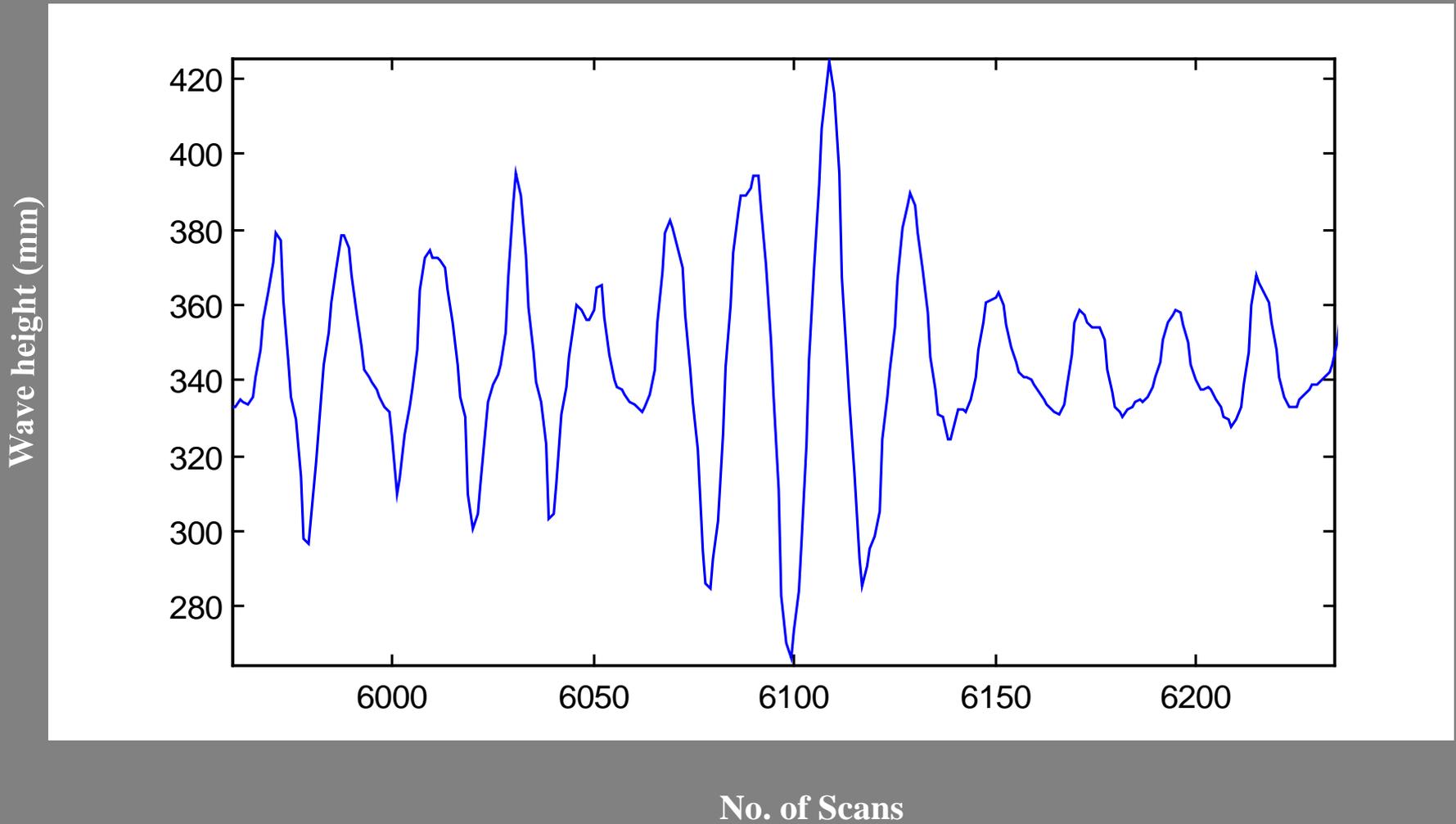


Wave Measurements

- Quirke Cell 14, 0.38 – 1.5 m
- Heath Steele Upper Cell
0.9 – 1.2 m



Time History of Surface Elevation

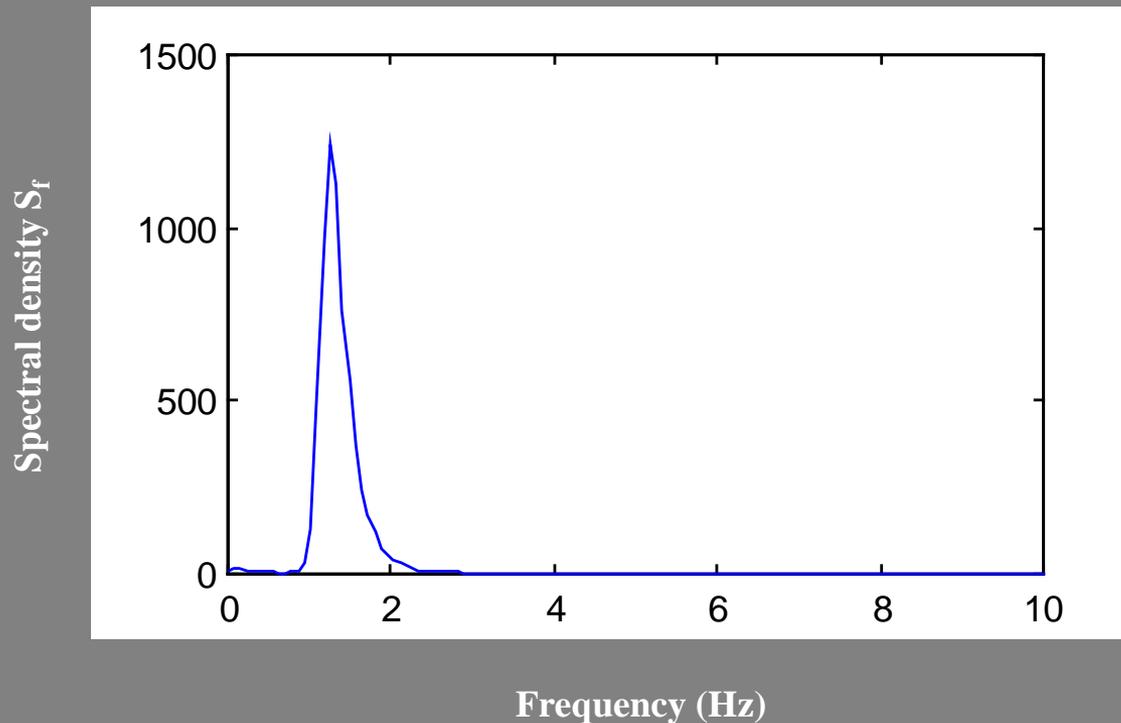


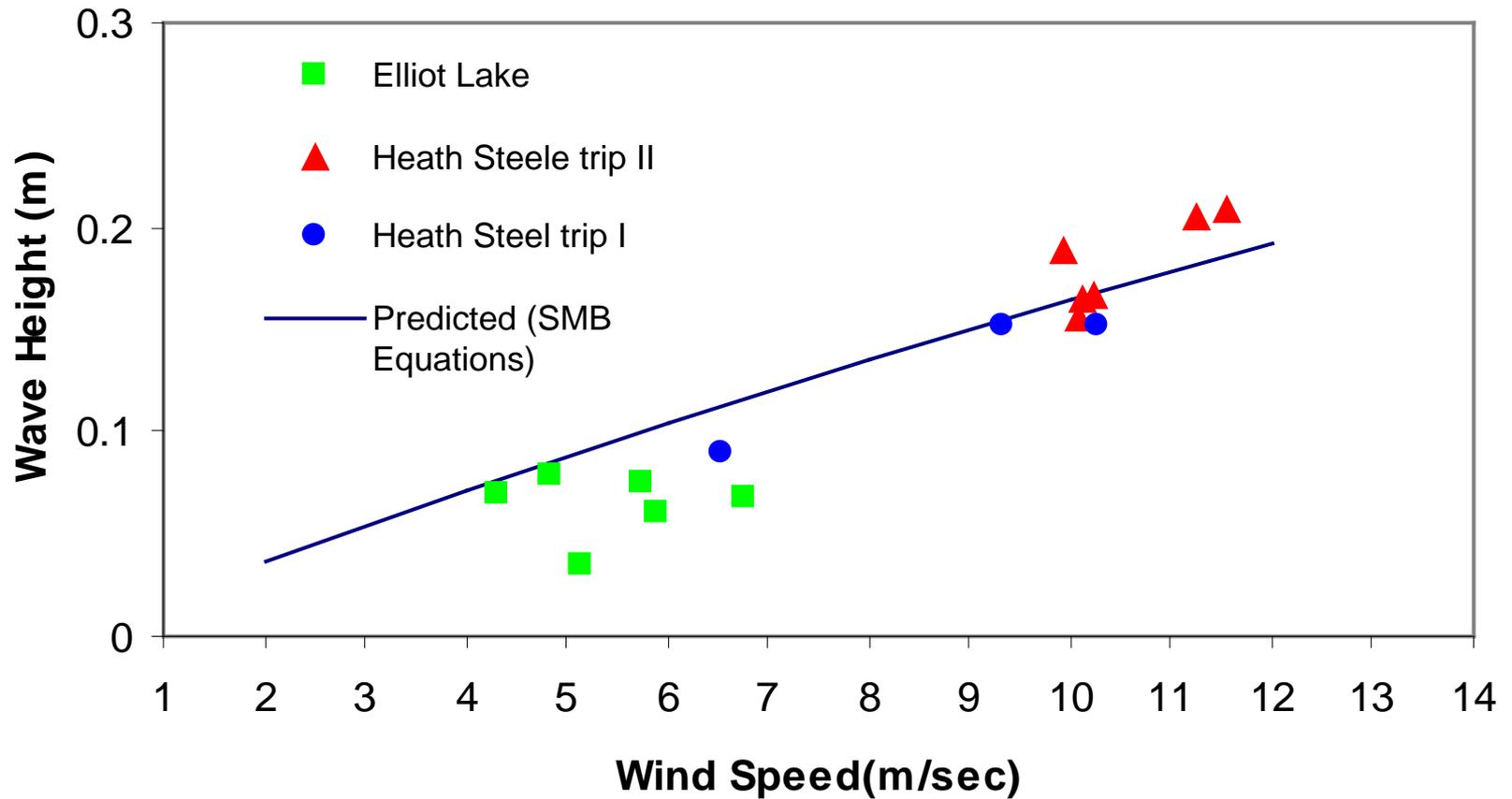
Data Processing

- Spectral analysis (root mean square approach)

$$H_s = 1.416 H_{rms} = 1.416 \sqrt{\sum_{i=1}^N H_i^2 / N} \approx 4 \sqrt{m_o} = 4 \sigma_n$$

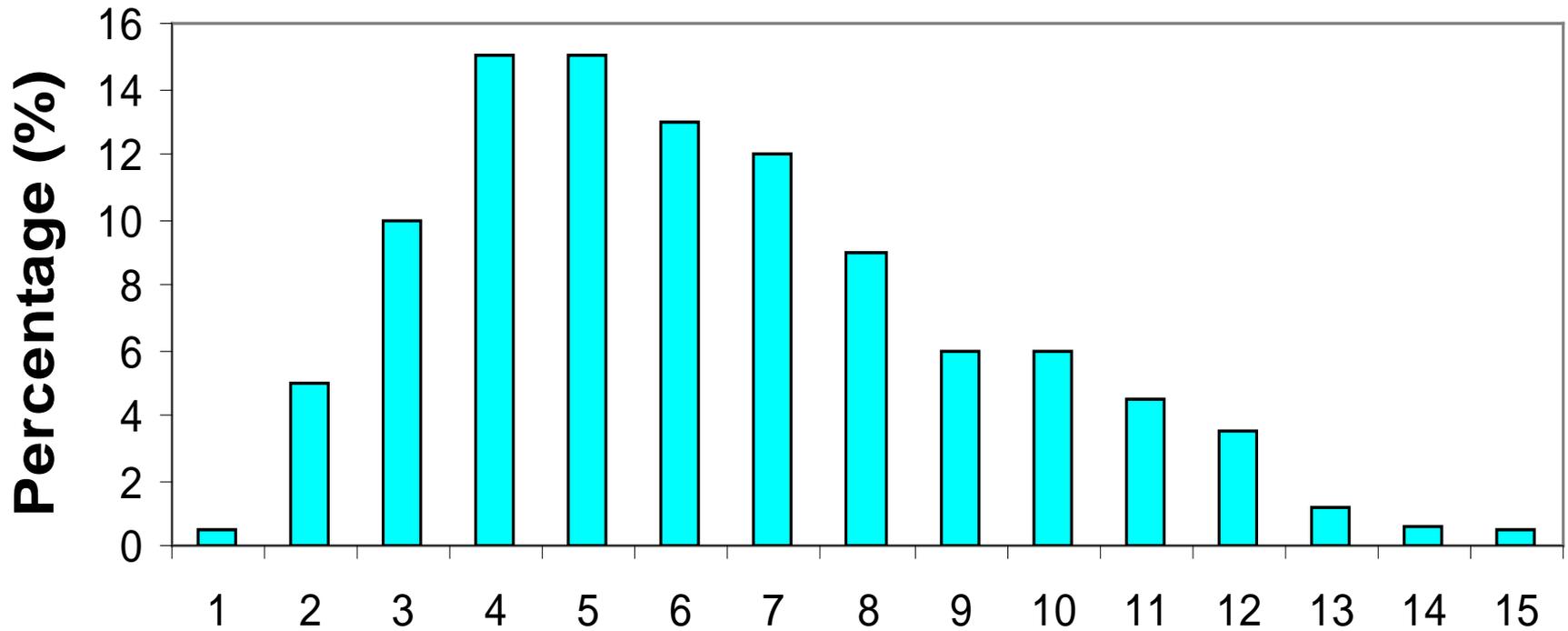
- H_s (significant wave height)





Measured and predicted wave heights for 1 m

Wind Frequency Diagram: Heath Steele



Wind Speeds for July 28-August 26, 1999

Grain Size Distribution

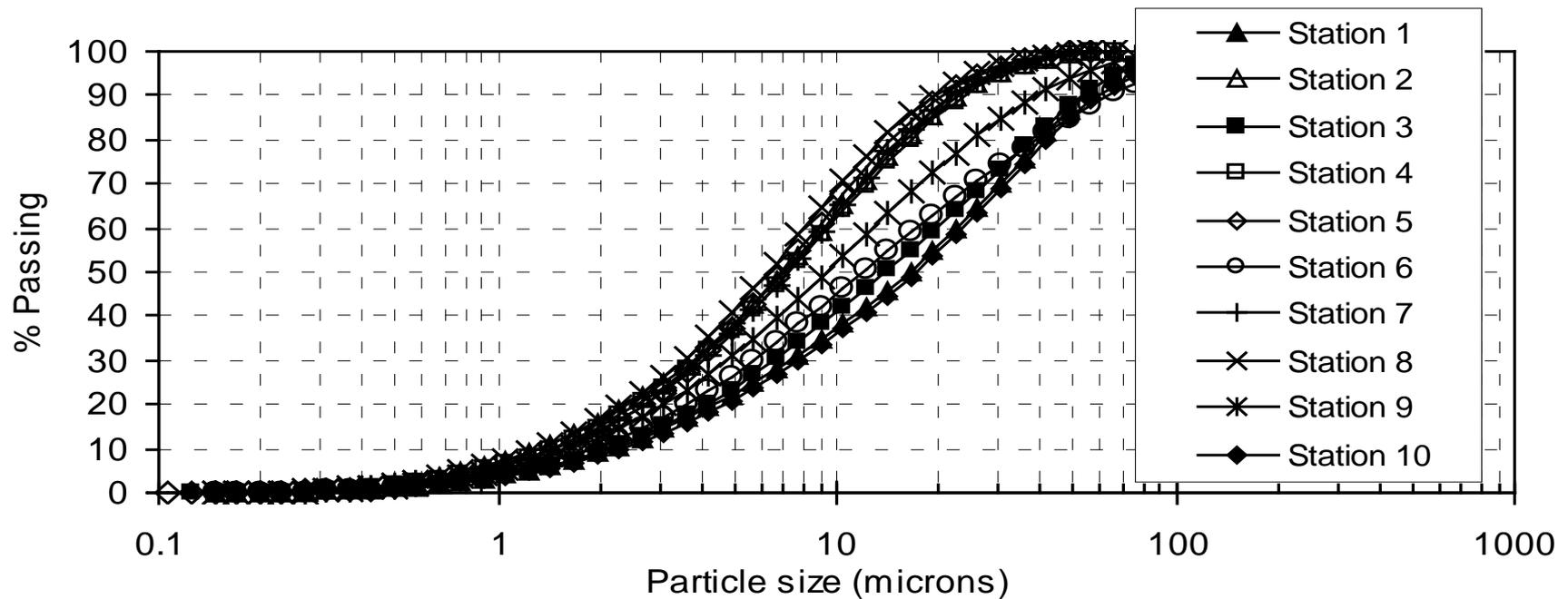
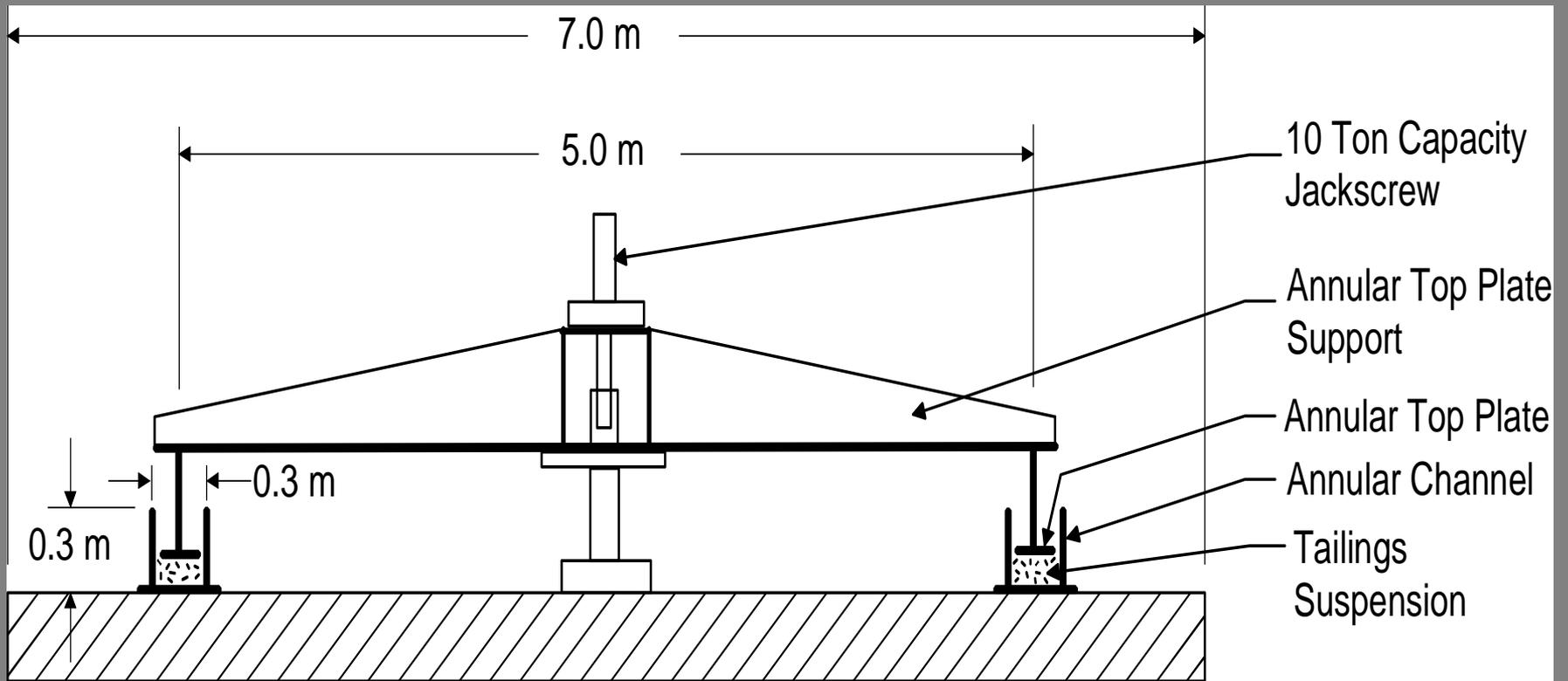
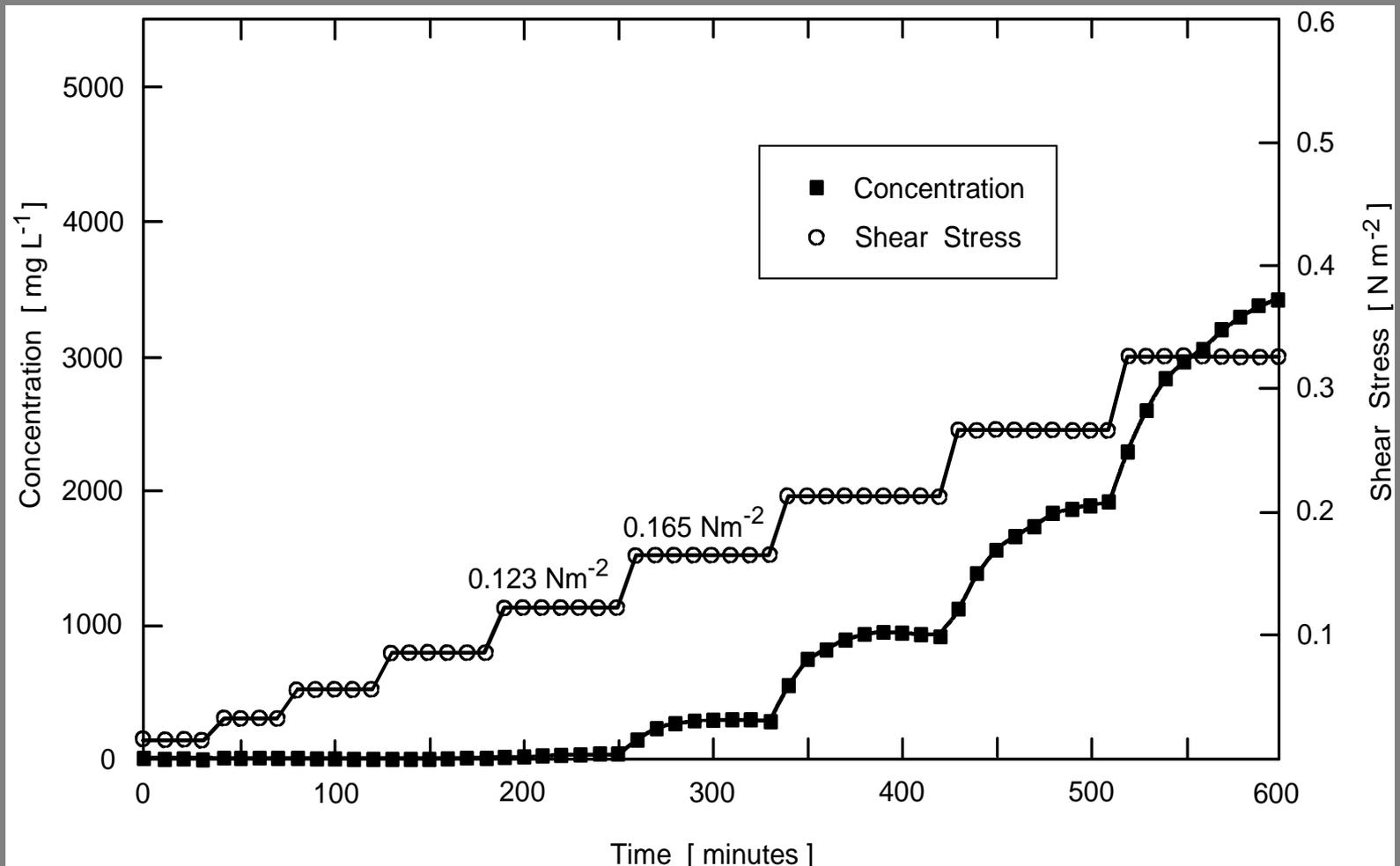


Figure 1 Particle size distributions of bed tailings at different stations (Heath Steele Upper Cell Pond)

Side View of Laboratory Annular Flume and Ring (Modified from Krishnappan, 1993)



Shear Stress and Suspended Tailings Concentration Measured in Rotating Flume



Plots Showing the Transition from Deep Water Wave to Shallow Water Wave Conditions in 0.75 m to 2 m Water Depth

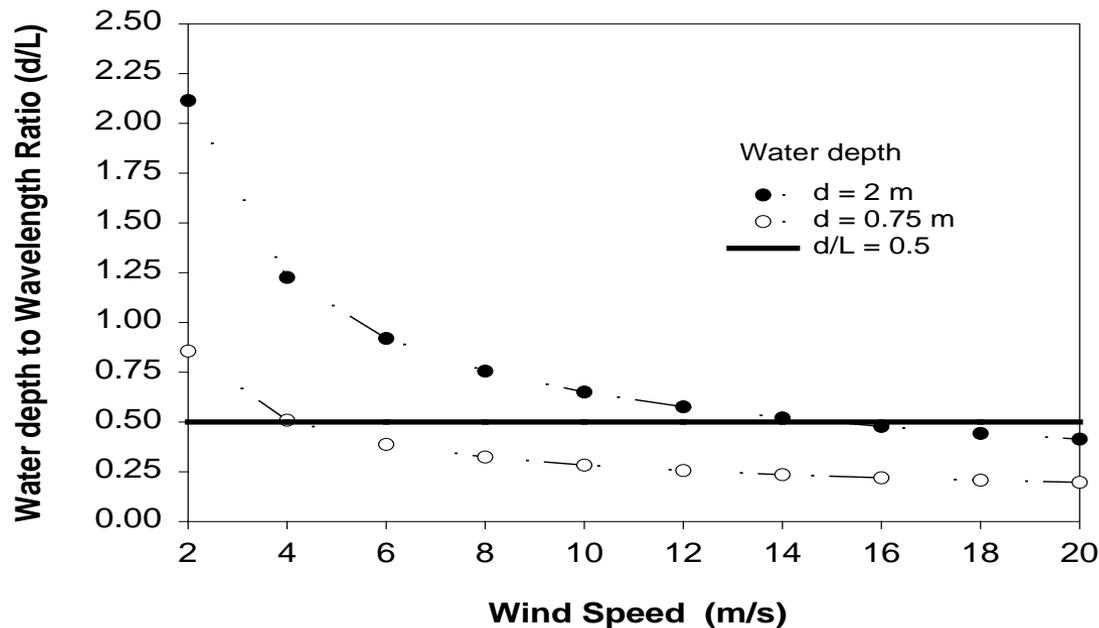


Figure 6 Plots showing transition from deep water wave ($d/L > 0.5$) to shallow water wave ($d/L < 0.5$) conditions in 0.75 m and 2 m water covers at different wind speeds

Comparison of Predicted Total Bed Shear Stress and Measured Shear Stress of Heath Steele Mine Tailings under 1 m Water Cover

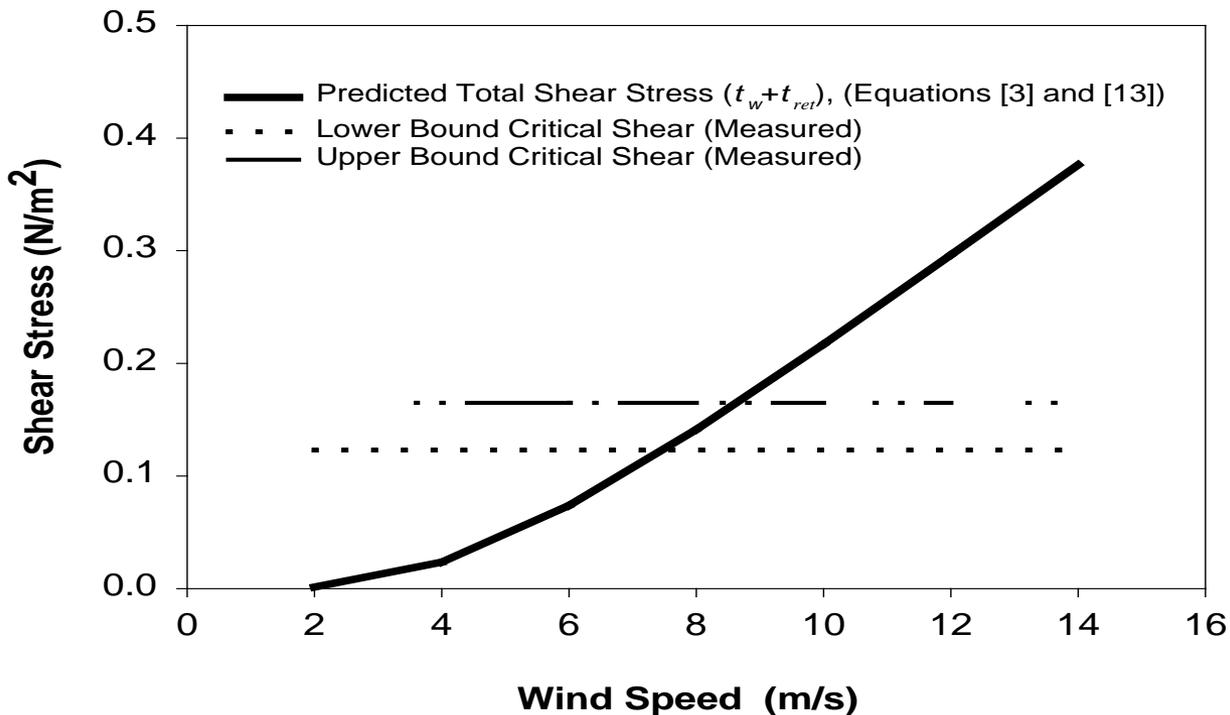


Figure 10 Comparison of predicted total bed shear stress under 1-m water cover and measured critical shear stress of Heath Steele mine tailings

Predicted Critical Wind Speed for Erosion versus Water Cover Depth (Heath Steele)

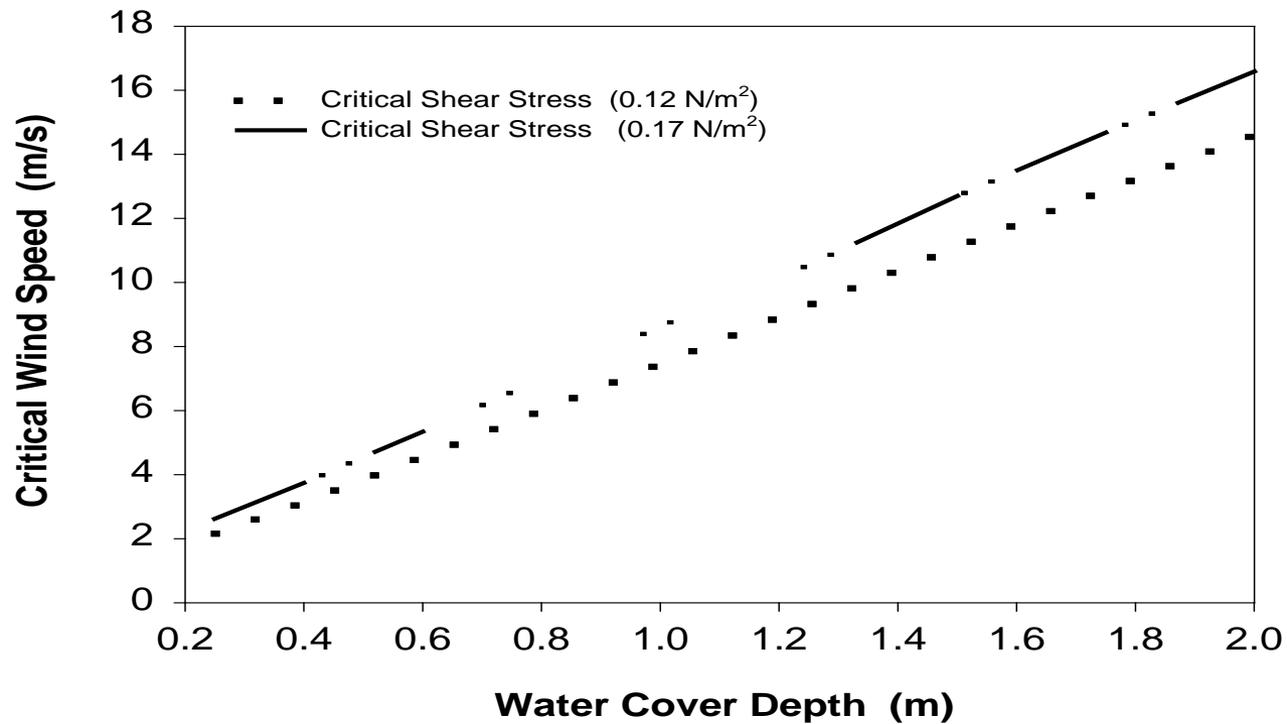
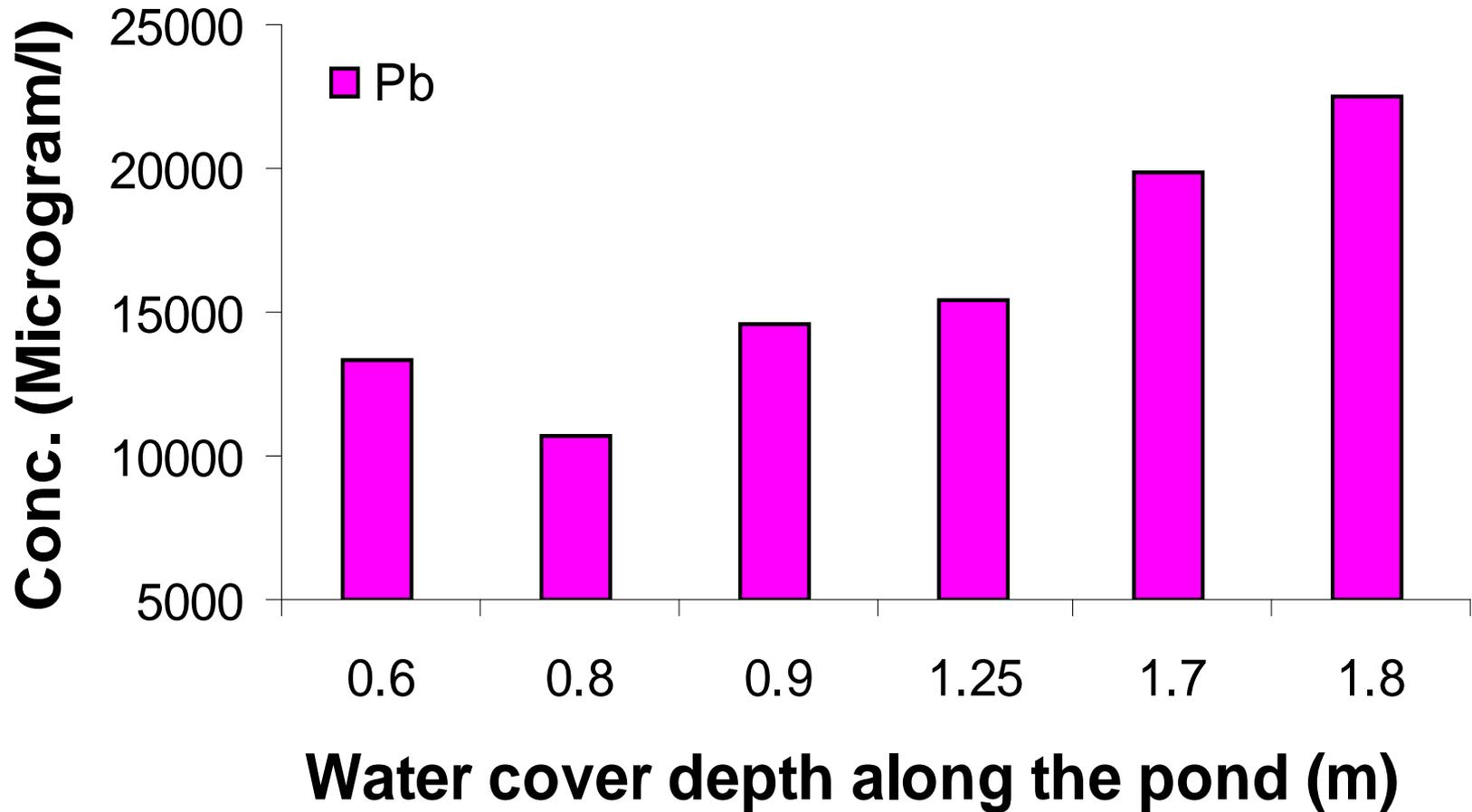
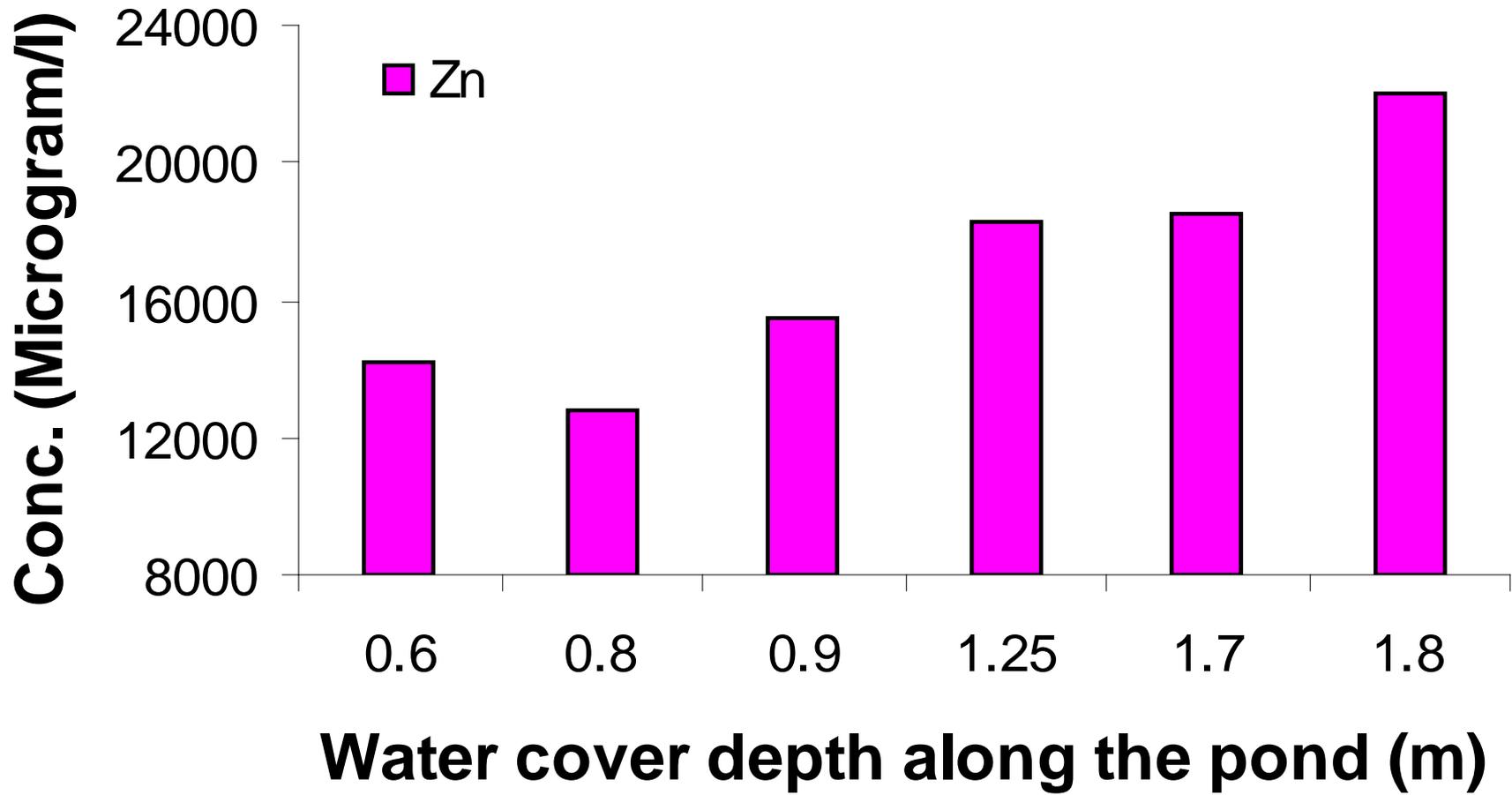


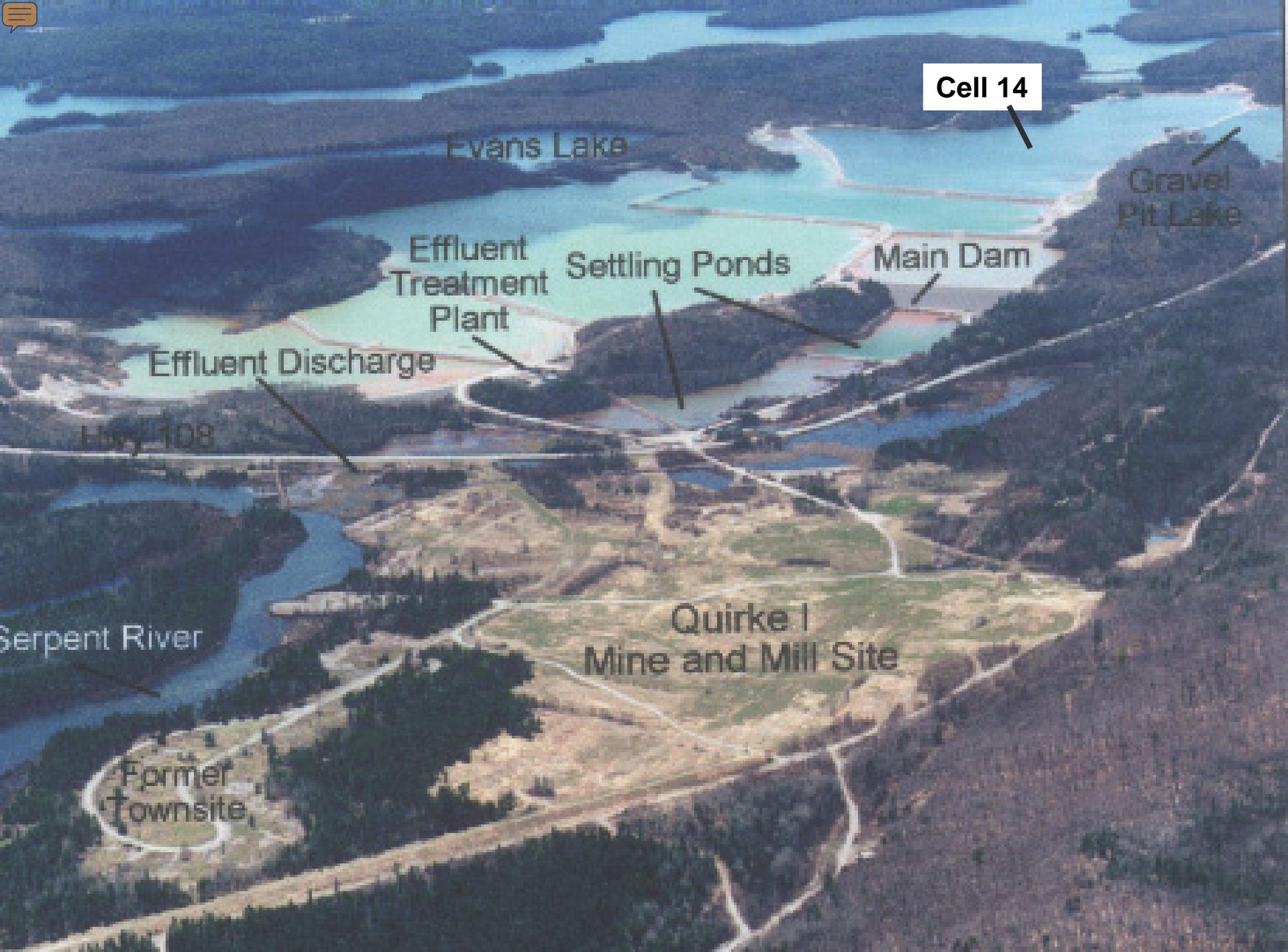
Figure 11 Predicted critical wind speed for erosion versus water cover depth (Heath Steele Mine Upper Cell tailings pond)

Metals as Tracers : Heath Steele Upper Cell









Cell 14

Evans Lake

Gravel Pit Lake

Effluent Treatment Plant

Settling Ponds

Main Dam

Effluent Discharge

Hwy 108

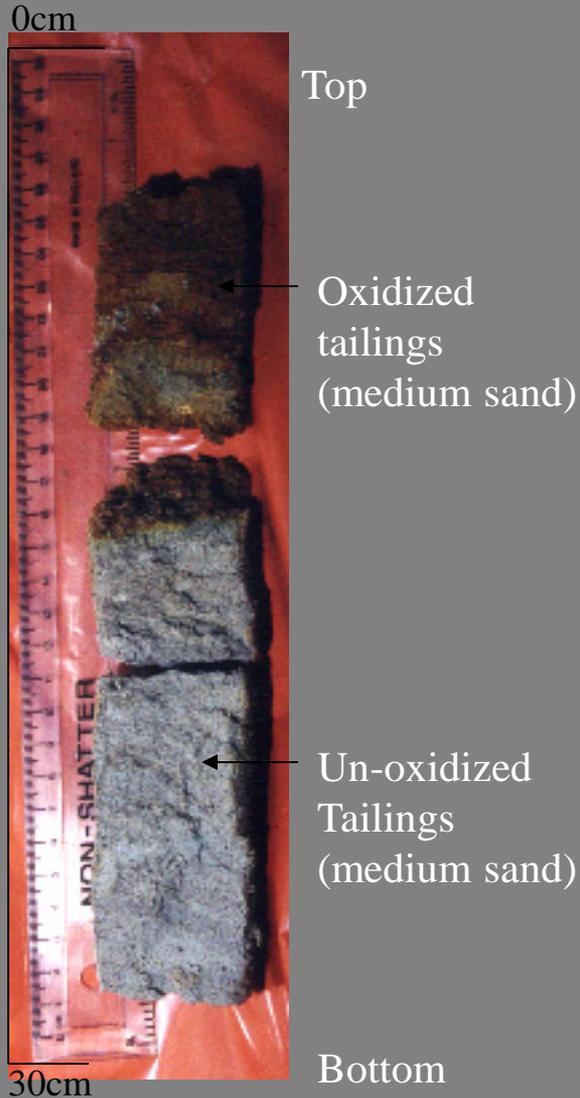
Serpent River

Quirke I Mine and Mill Site

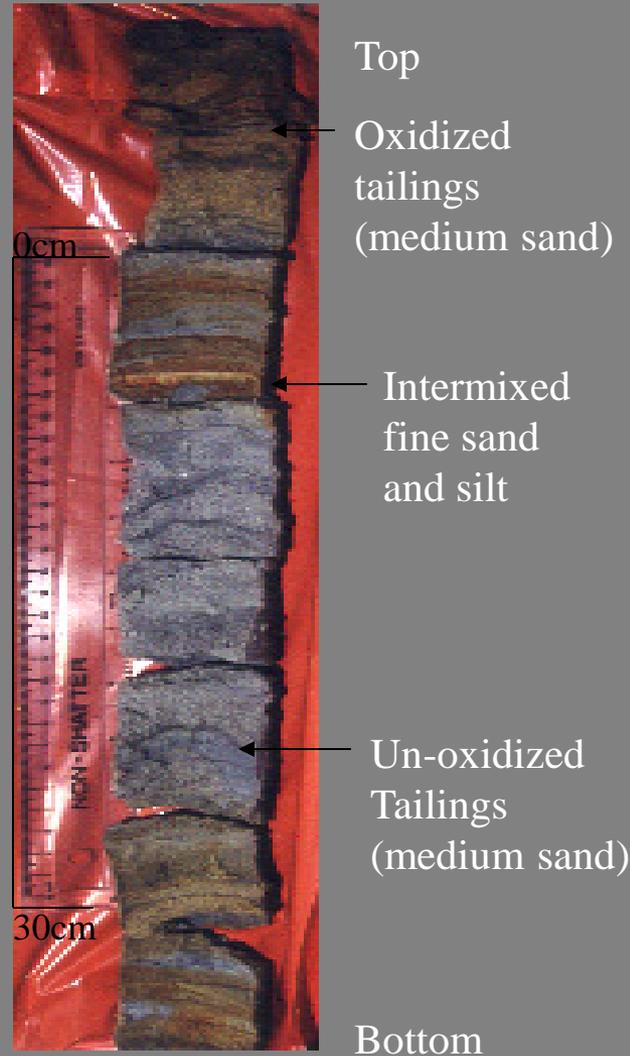
Former Townsite

Solid Tailings Analysis

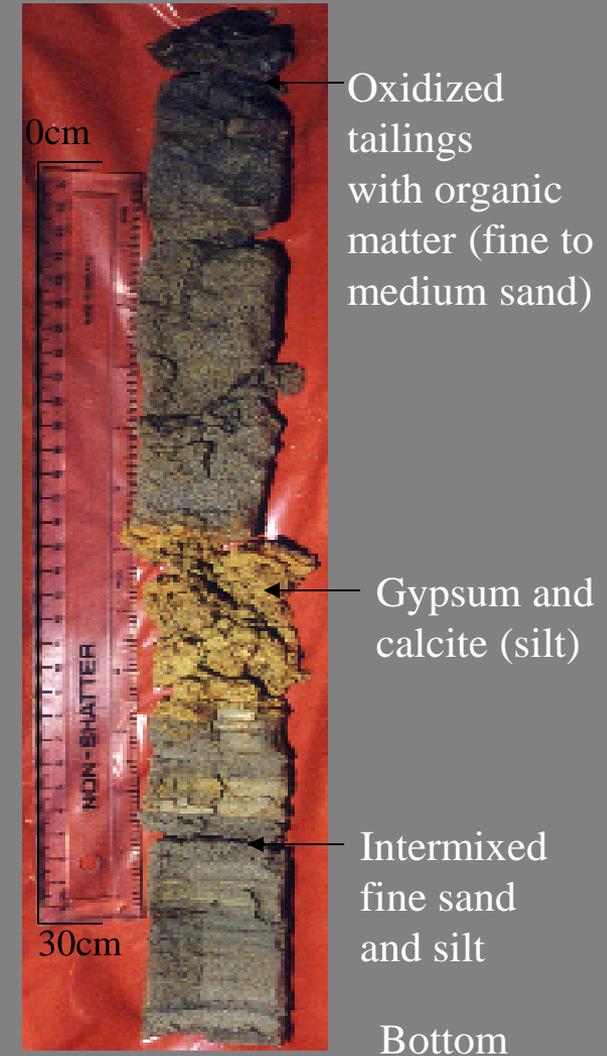
Station 1



Station 3



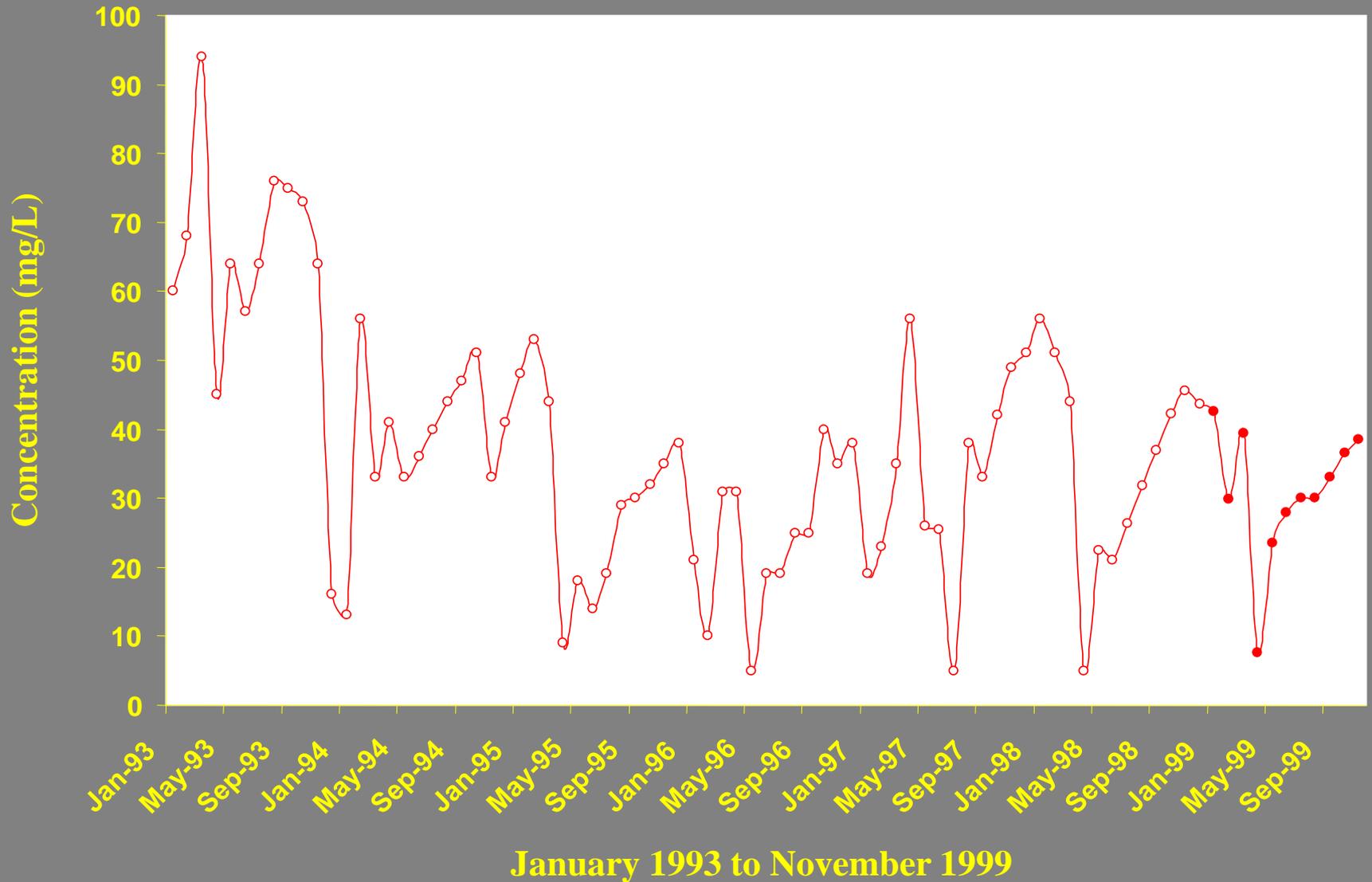
Station 6



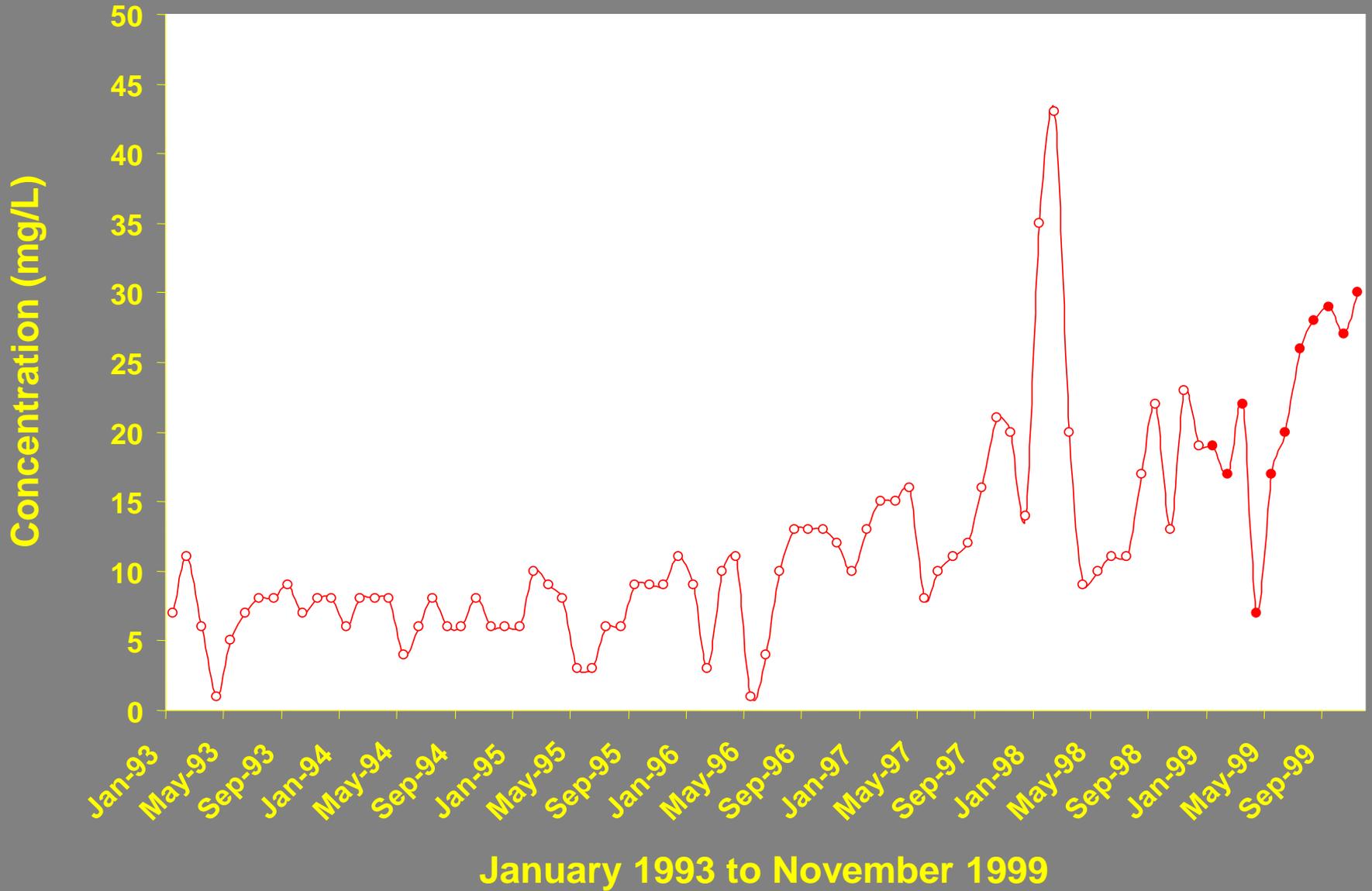
Mineralogical Analysis

Station Number	Main Mineral	Sulphide Mineral	Secondary Mineral	Trace or Minor
1	Quartz (88 to 95%) K-Feldspar (1 to 8%) Muscovite (1 to 3%)	Pyrite (2 to 8%)	Gypsum (2 to 17%) Calcite (1 to 17%)	Chalcopyrite Rutile Illmenite
3	Quartz (65 to 98%) K-Feldspar (3 to 10%) Muscovite (1 to 4%)	Pyrite (1 to 2%)	Gypsum (1 to 4%)	Chalcopyrite Rutile
6	Quartz (69 to 91%) K-Feldspar (3 to 11%) Muscovite (1 to 8%)	Pyrite (2 to 8%)	Gypsum (4 to 18%)	Chalcopyrite Rutile

SO₄ Concentration (mg/L)

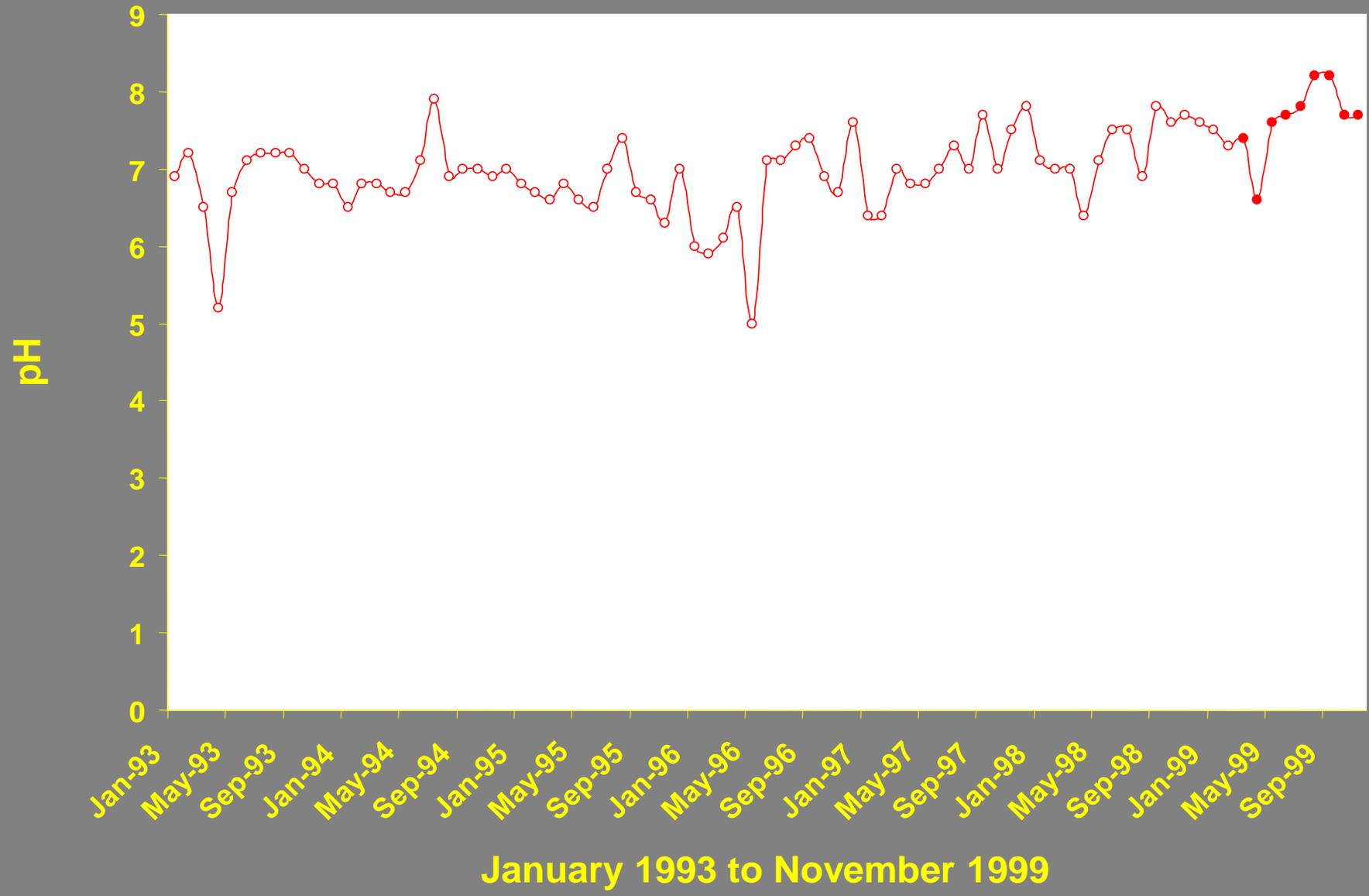


Alkalinity as CaCO_3 (mg/L)

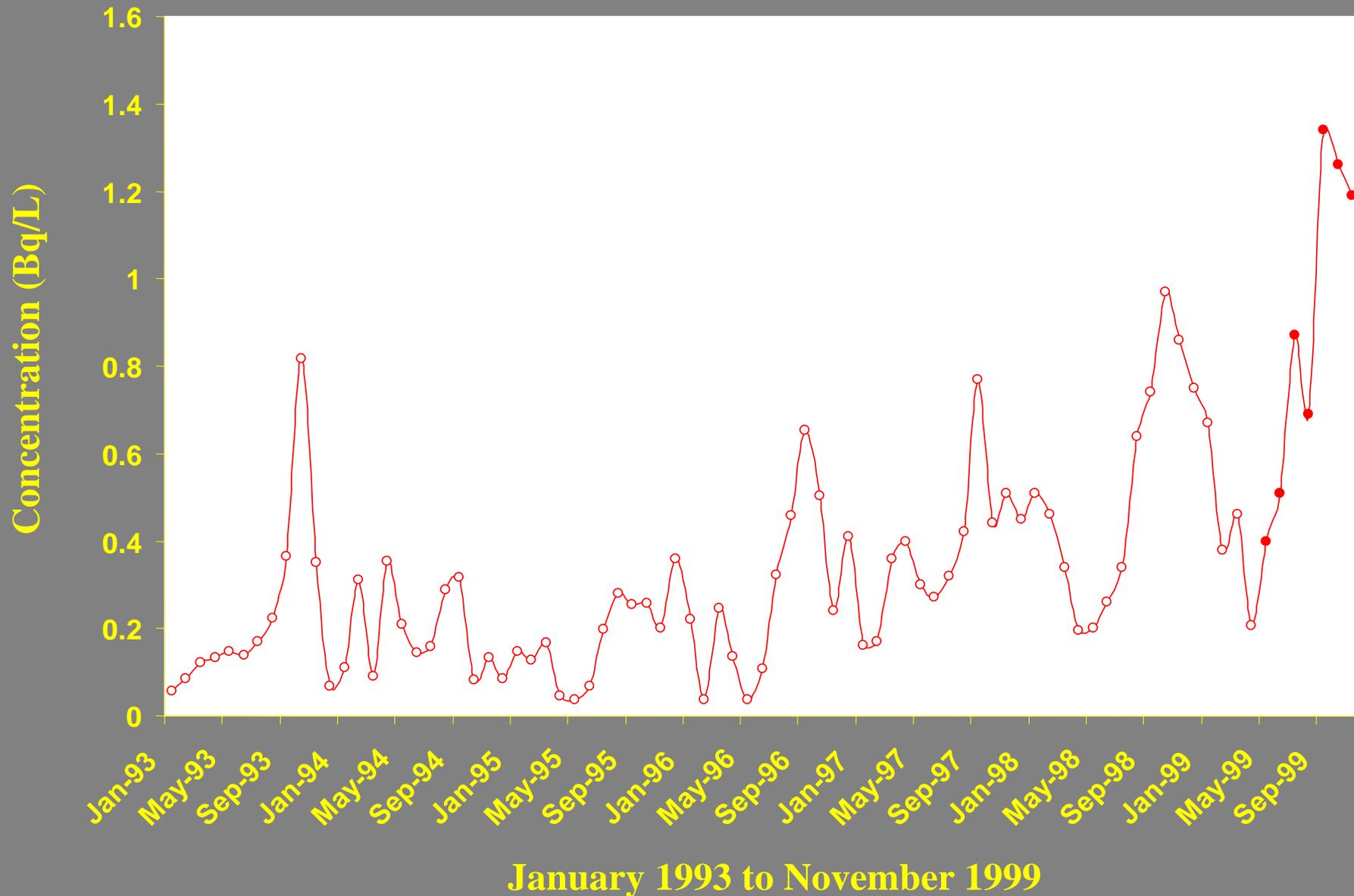




pH



Ra-226 Concentration (Bq/L)





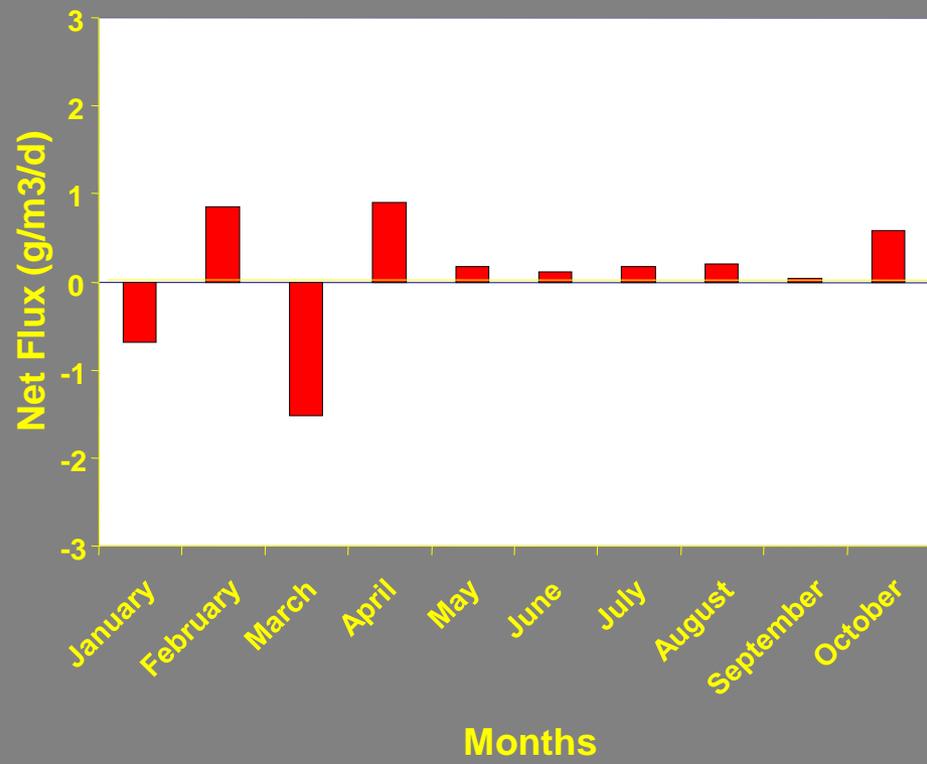
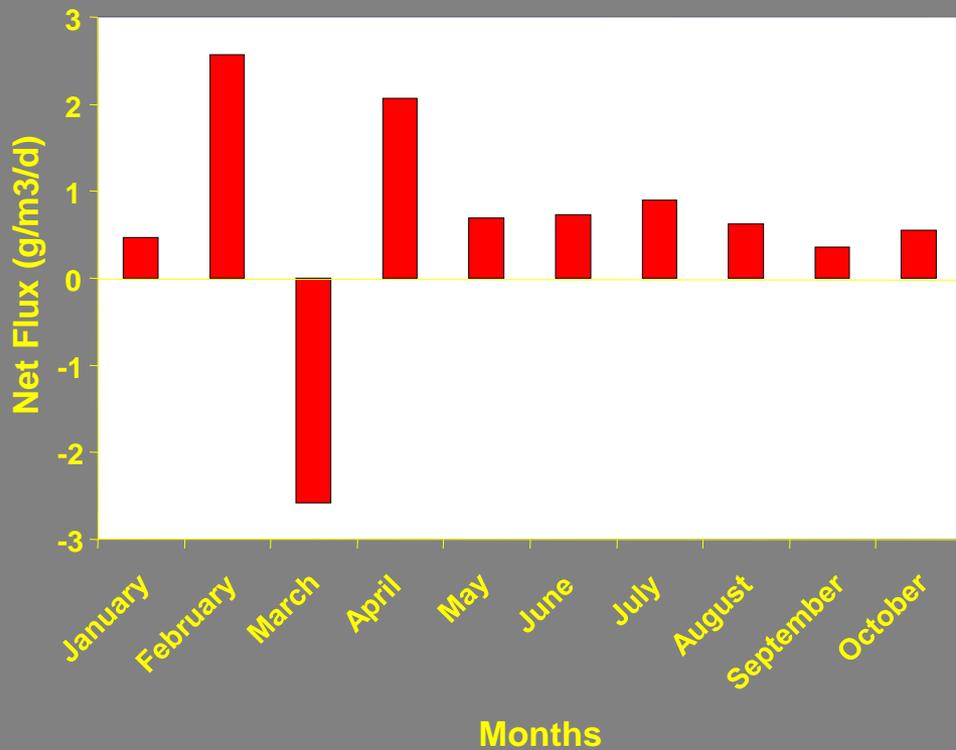
Seepage Loss Analysis

- Golders Associates
- $SL=P-E-H$
- Fresh water inflow from Gravel Pit Lake to maintain operating elevation of 1310ft
- Factored Precipitation 0.7
- Class A pan evaporation of 0.85
- Dyke 14, two perimeter dams (K1 and K2) and an old landfill
- Seepage for 1993 and 1999 are: 56.1L/sec and 40L/sec

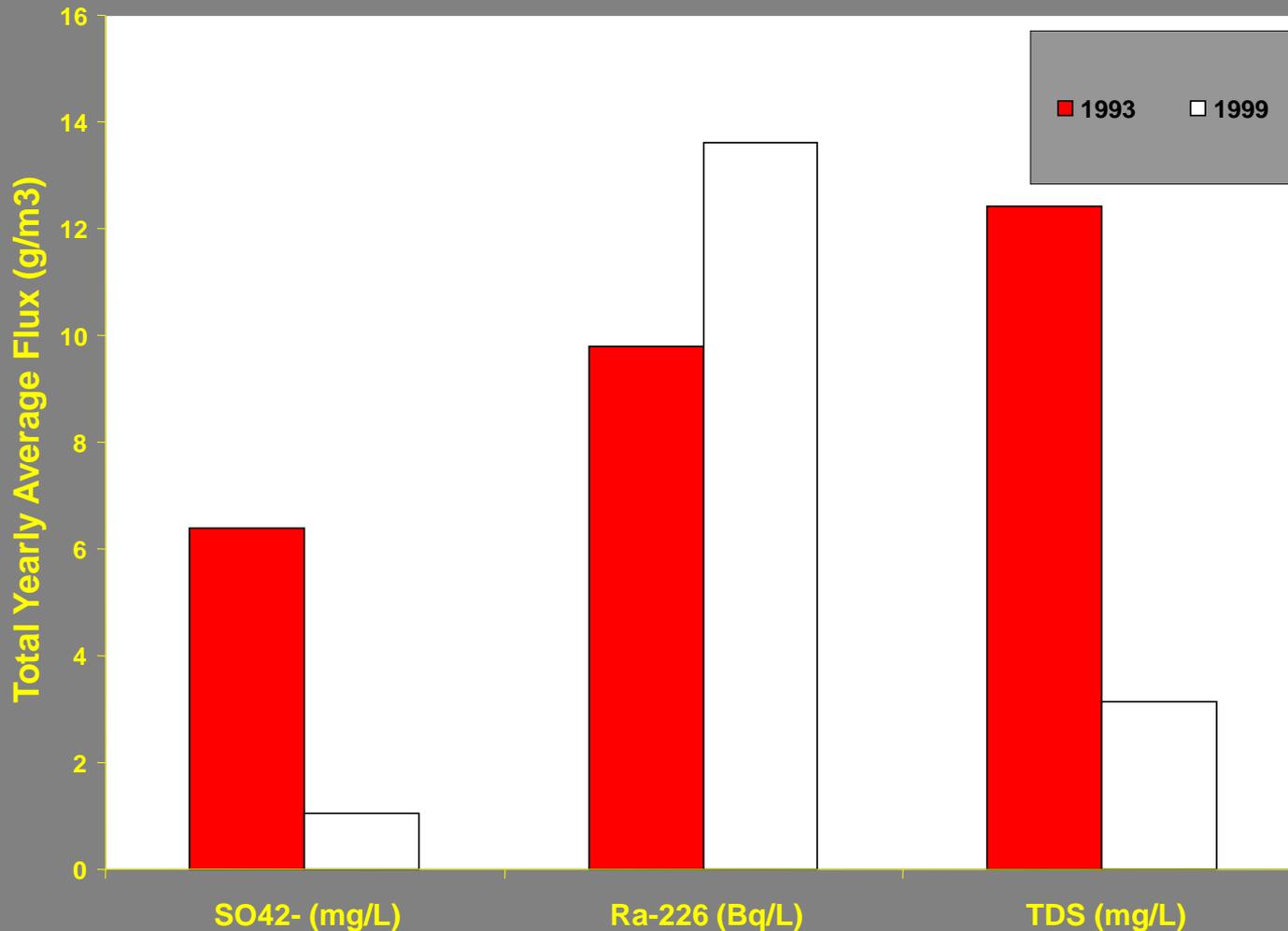
Fluxes in the Water Cover

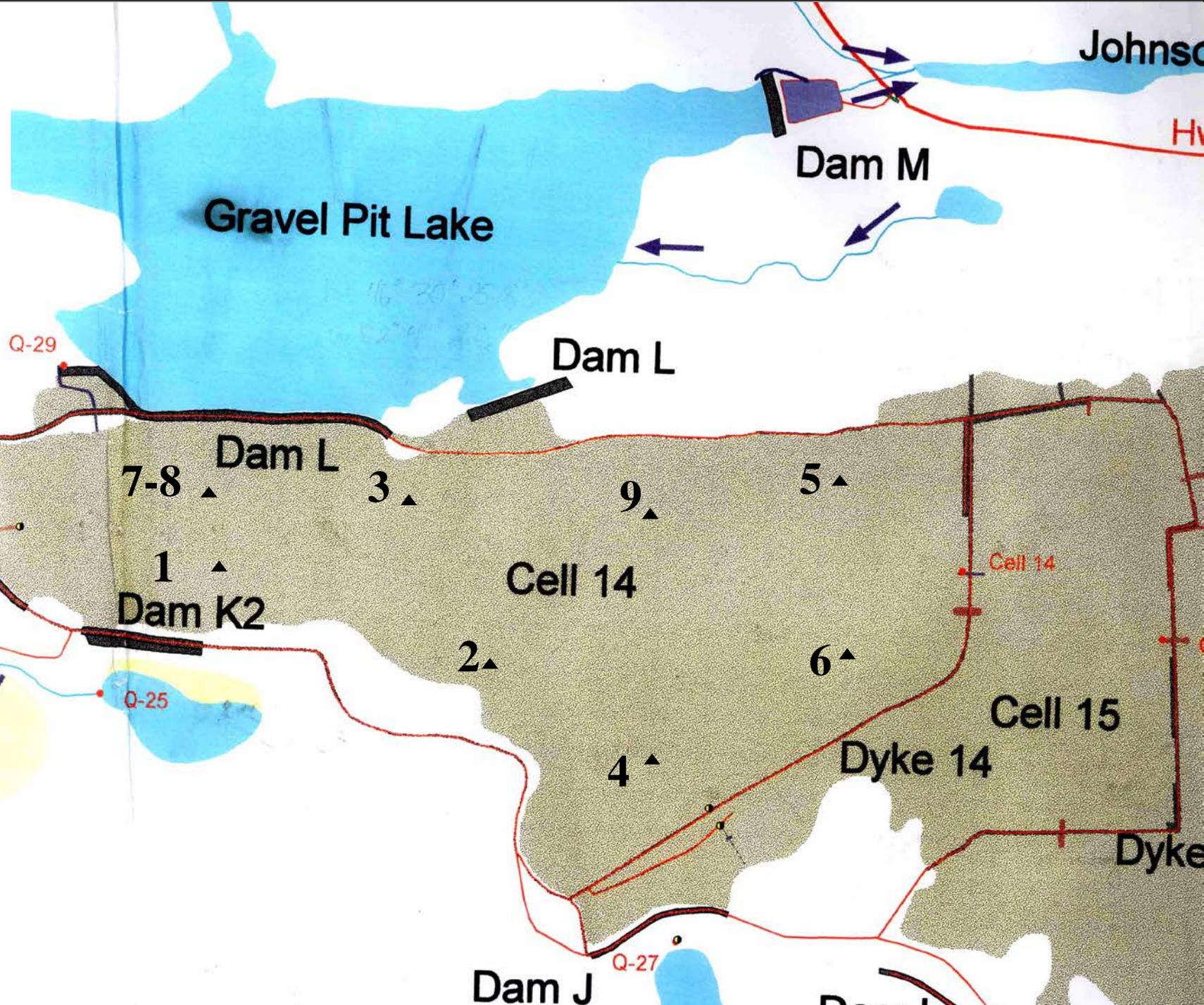
- Fluxes calculated using the method developed by Catalan, Yanful and St.Arnaud (1999) for Preoxidized Tailings.
- $F_T = F_A + F_N$
- $M_W(t_2) - M_W(t_1) = F_T \Omega \cdot (t_2 - t_1)$
- $F_A = -[1 / \Omega \cdot (t_2 - t_1)] \int_{t_1}^{t_2} SC_W \cdot dt$
- $F_N = 1 / \Omega \cdot (t_2 - t_1) [M_W(t_2) - M_W(t_1) + \int_{t_1}^{t_2} SC_W \cdot dt]$

1993 and 1999 Net Flux of SO_4^{2-}



Net Yearly Average Flux of SO_4^{2-} , Ra-226, and TDS





Gravel Pit Lake

Dam M

Dam L

Dam K1

Dam L

Dam K2

Cell 14

Cell 14

Cell 15

Dyke 14

Dyke

Dam J

Q-29

Q-25

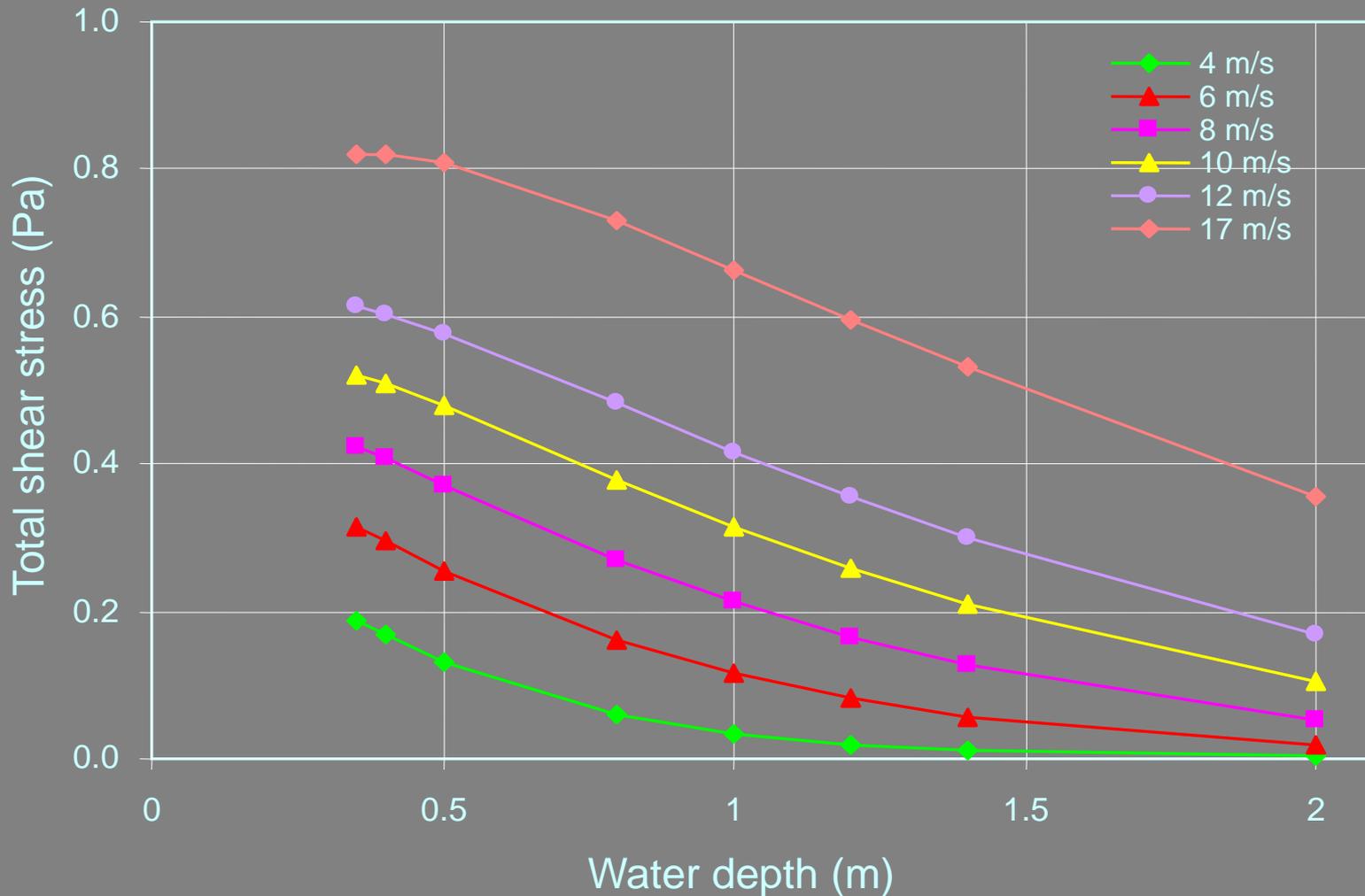
Q-27

Johnso

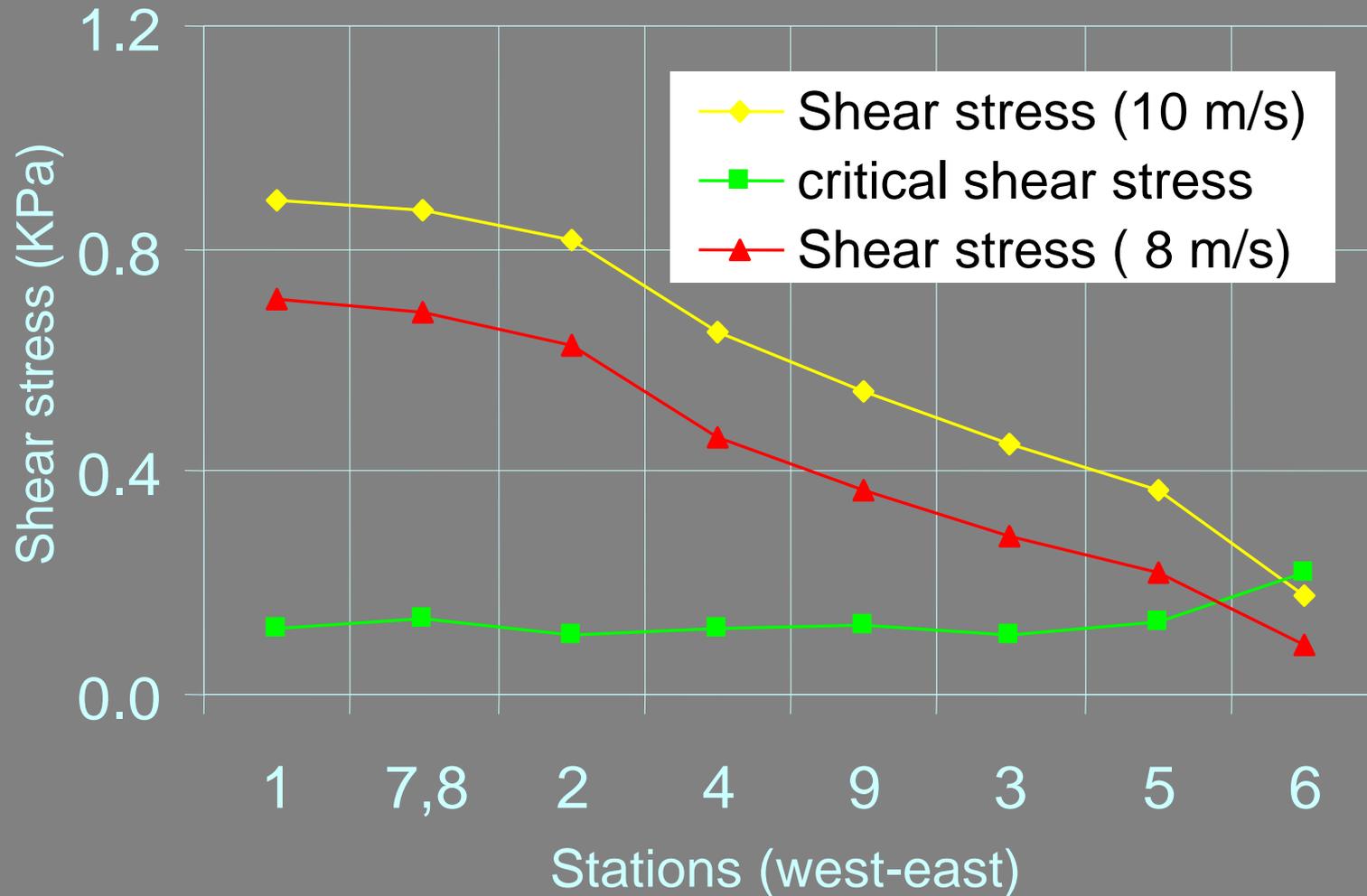
Hv



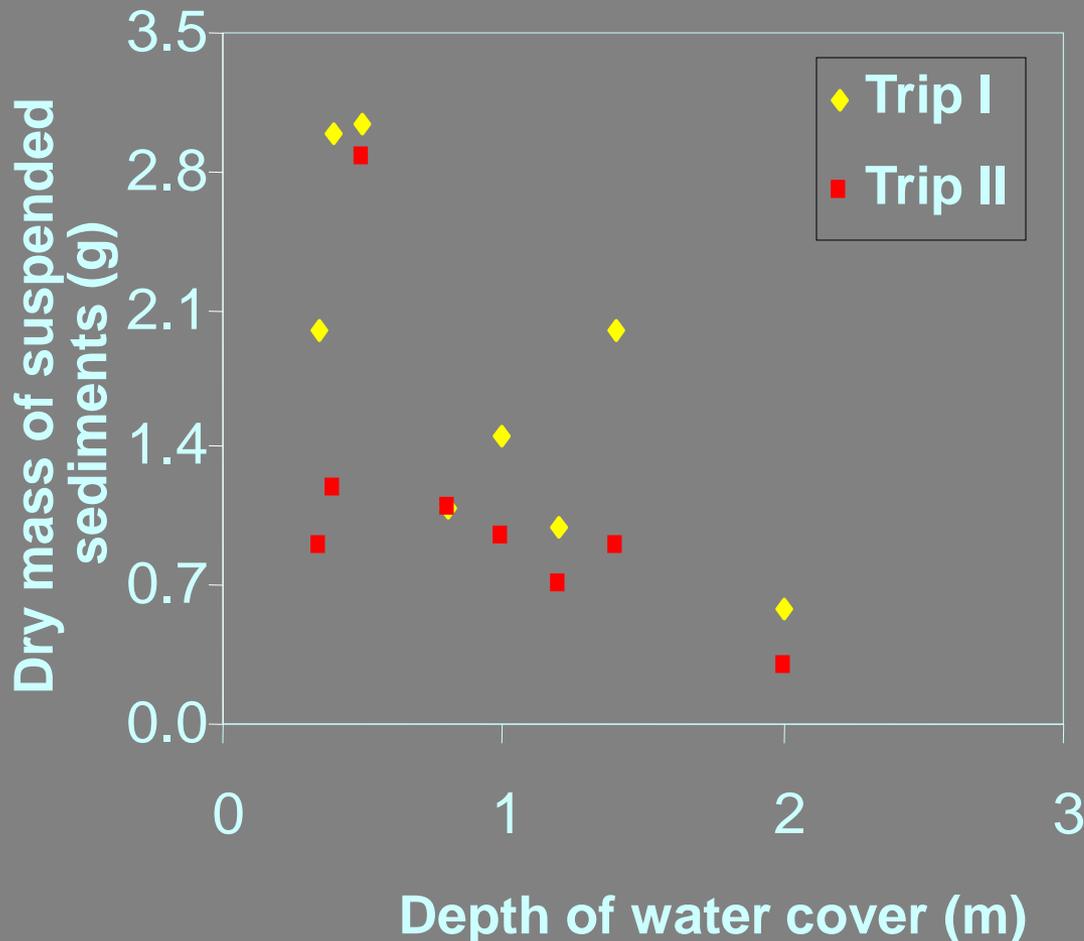
Predicted bed shear stress



critical shear stress

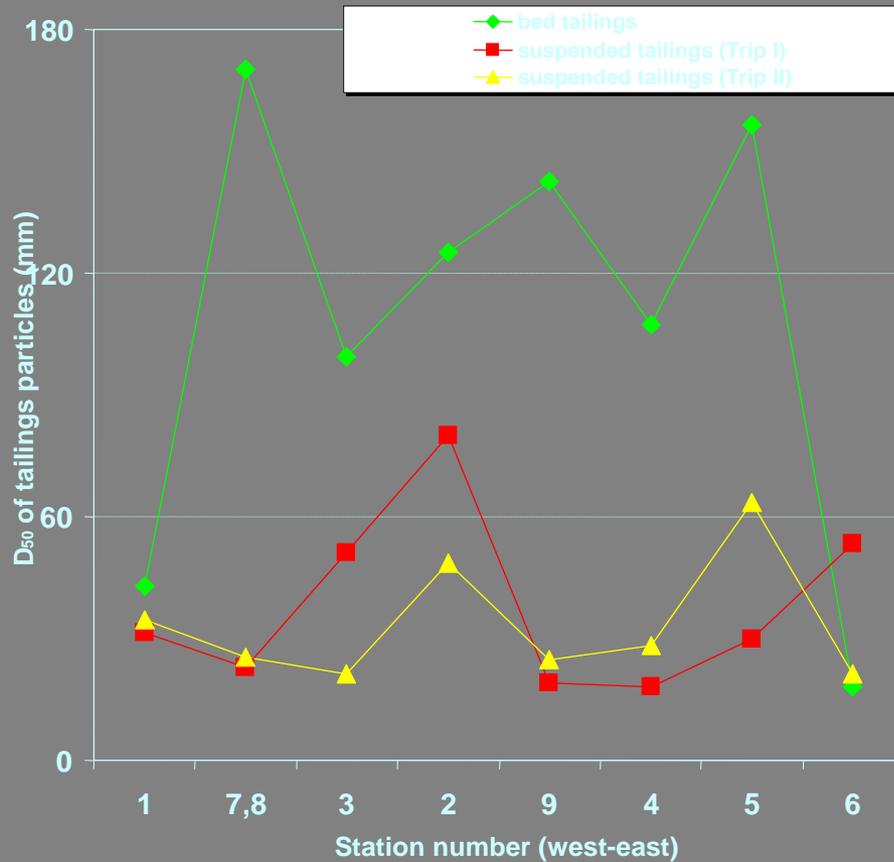


Dry mass of suspended sediments at different depths

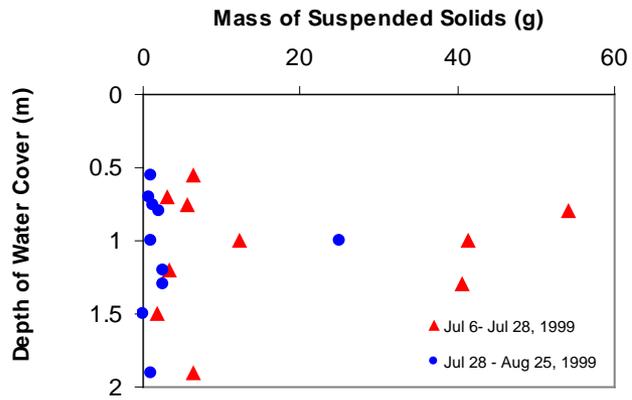


- mass of suspended solids decrease with increasing water depth.

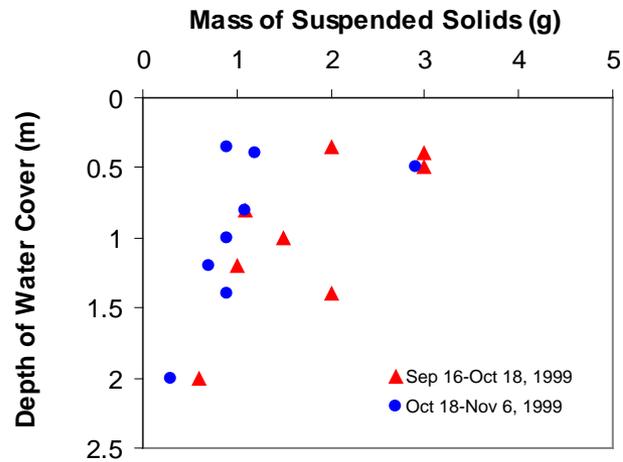
Comparison of D_{50} of bed and suspended tailings



- Particle sizes of the suspended tailings were much finer than that of the bed tailings.
- Suspended tailings for Trip II were coarser than for Trip I, (stronger wind conditions, creating higher bottom stresses).



**Heath Steele
Upper Cell**



Quirke Cell #14

Mineralogical composition of bed and suspended tailings

Minerals	Chemical composition	Percentage estimation	
		Bed tailings	Suspended tailings
Quartz	SiO_2	90	93
Mica	$\text{KAl}_2\text{AlSi}_3\text{O}_{10}(\text{OH})_2$	2.5	1.3
Calcite	CaCO_3	3.5	0.25
Pyrite	FeS_2	1.5	1
Feldspar	KAlSi_3O_8	3.5	3.9

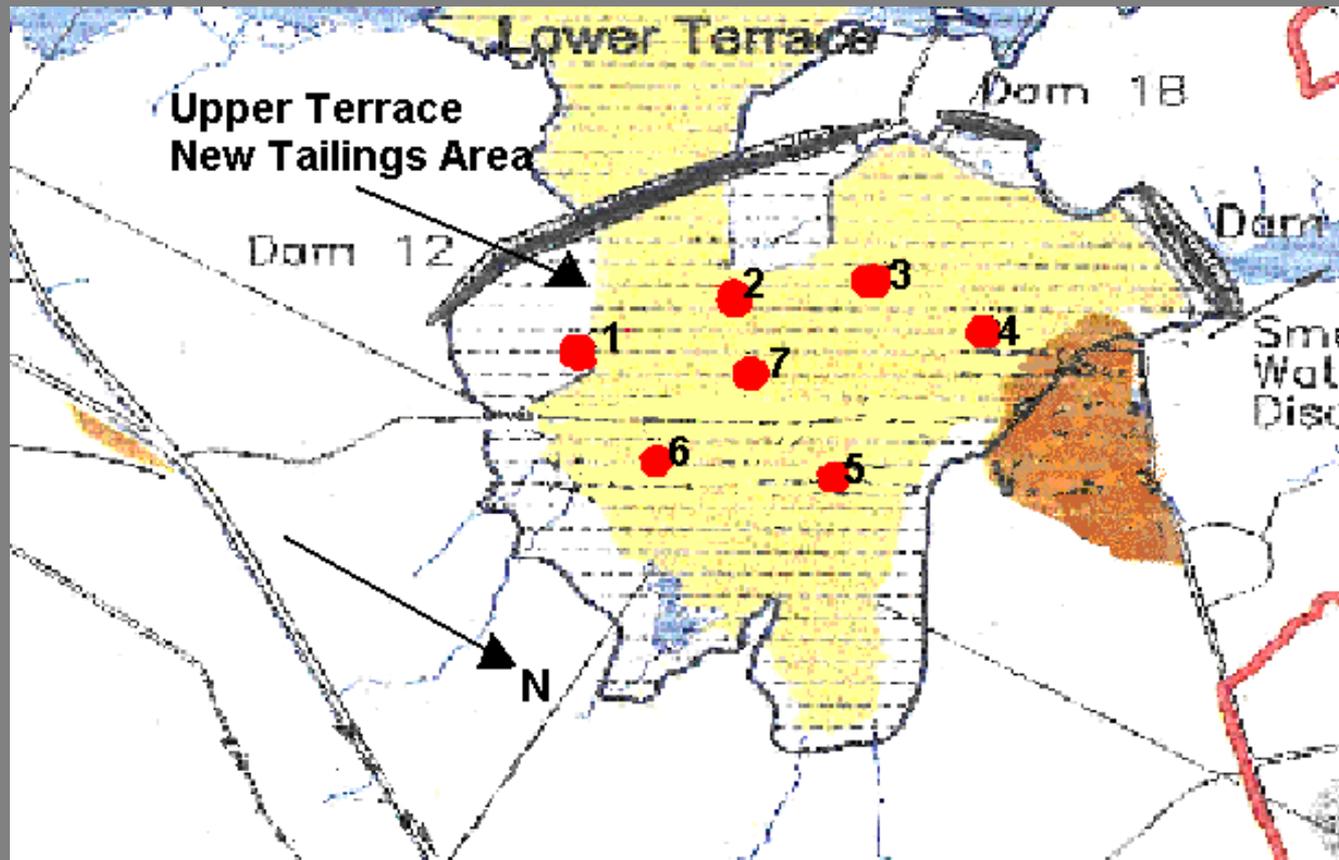
Elemental composition of bed and suspended tailings

Bed tailings																		
Station	Si	Ti	Al	Fe	Mn	Mg	Ca	K	P	Na	Cd	Cu	Ni	Pb	Zn	S	Th	U
1	397979	2618	22985	23641	129	3417	1644	18402	626	0	1	57	19	191	21	16563	97	18

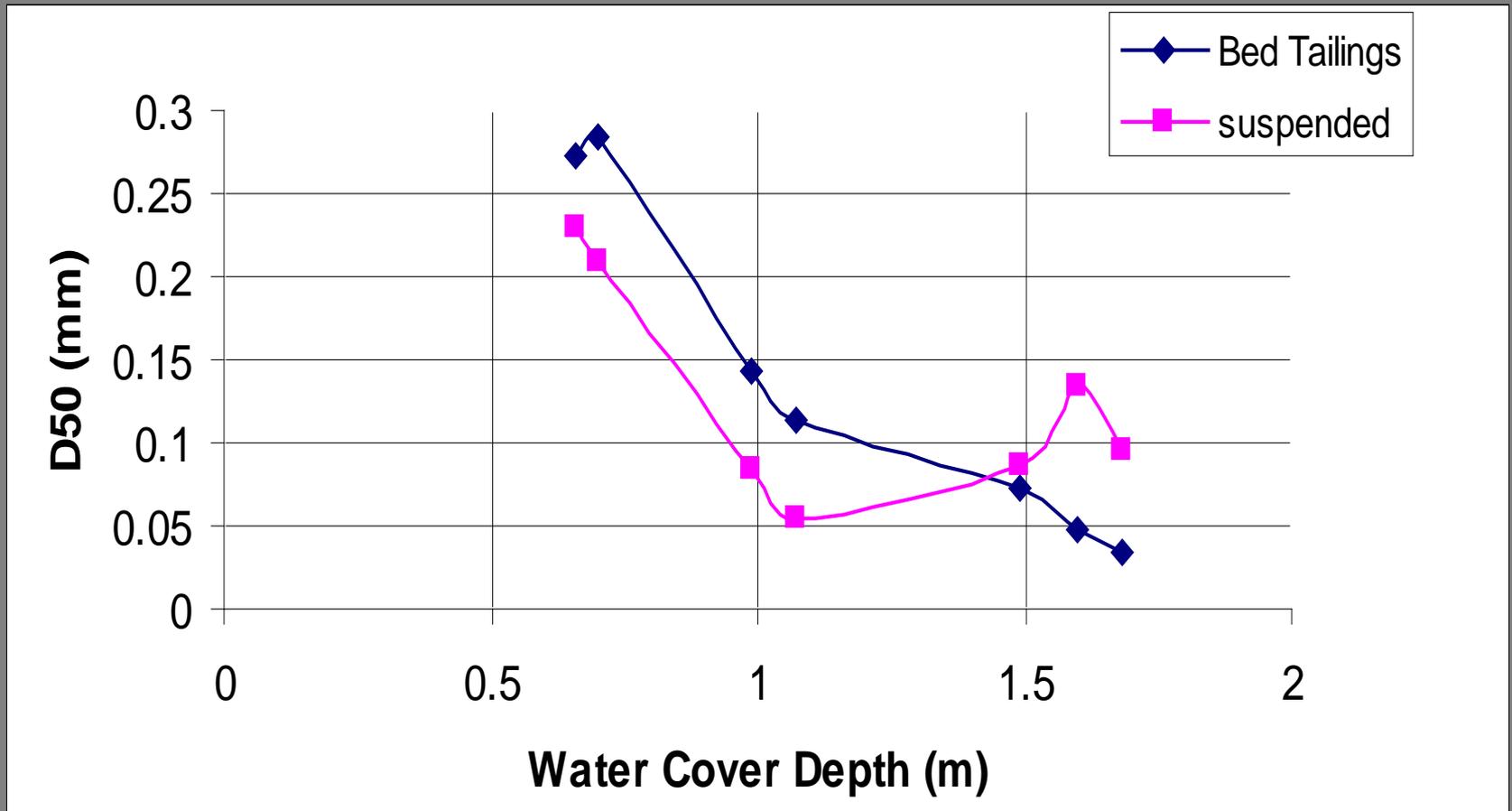
Suspended sediments (Trip I)																		
Station	Si	Ti	Al	Fe	Mn	Mg	Ca	K	P	Na	Cd	Cu	Ni	Pb	Zn	S	Th	U
1	310959	2338	29712	78337	1239	2593	1715	19675	393	0	3	234	42	946	484	25880	264	55

Suspended sediments (Trip II)																		
Station	Si	Ti	Al	Fe	Mn	Mg	Ca	K	P	Na	Cd	Cu	Ni	Pb	Zn	S	Th	U
1	334598	2878	28335	53087	1007	2231	18511	19342	175	0	1	120	45	673	104	10910	262	42

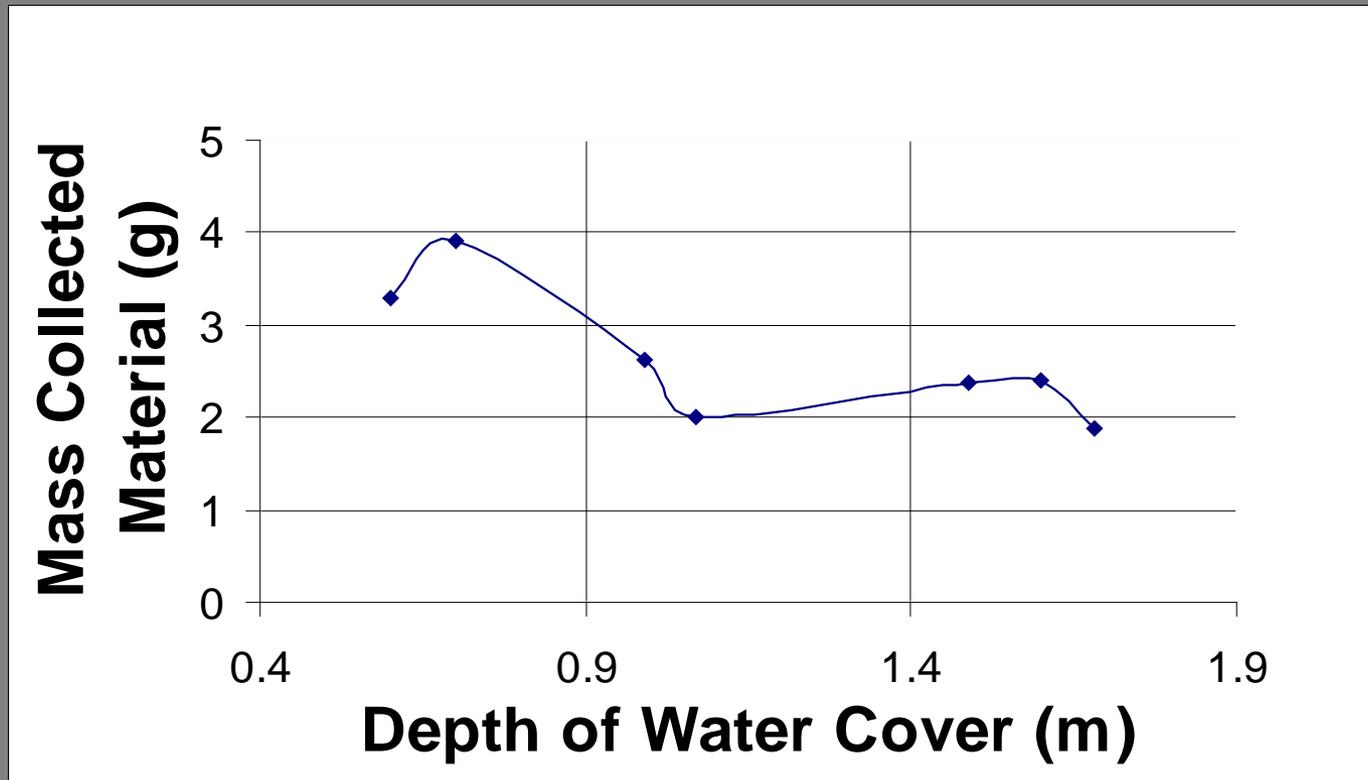
New Tailings Area (Upper Terrace)



Depth of Water Cover vs Average Grain Size



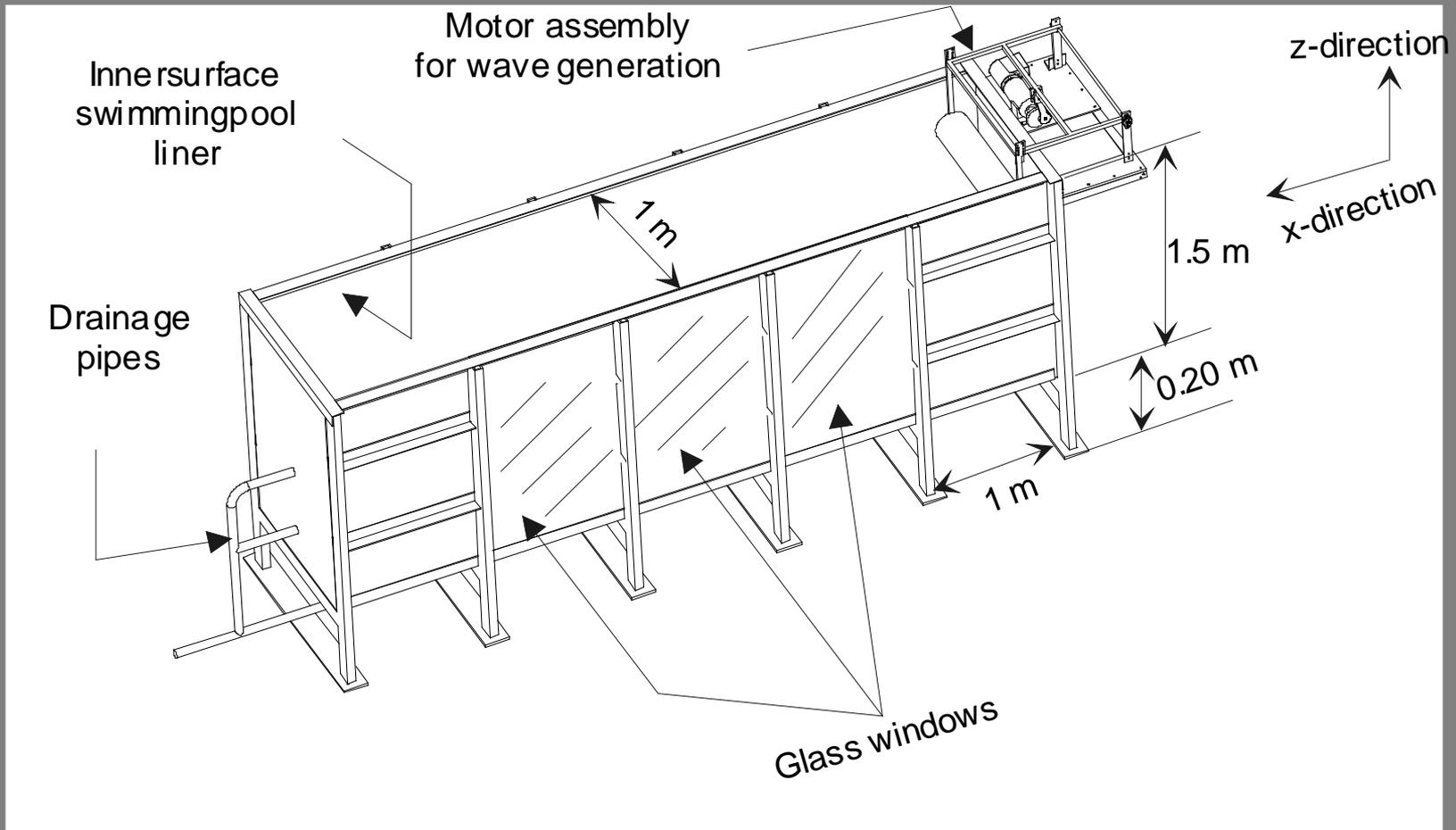
Total Mass of Collected Material with Depth of Water Cover



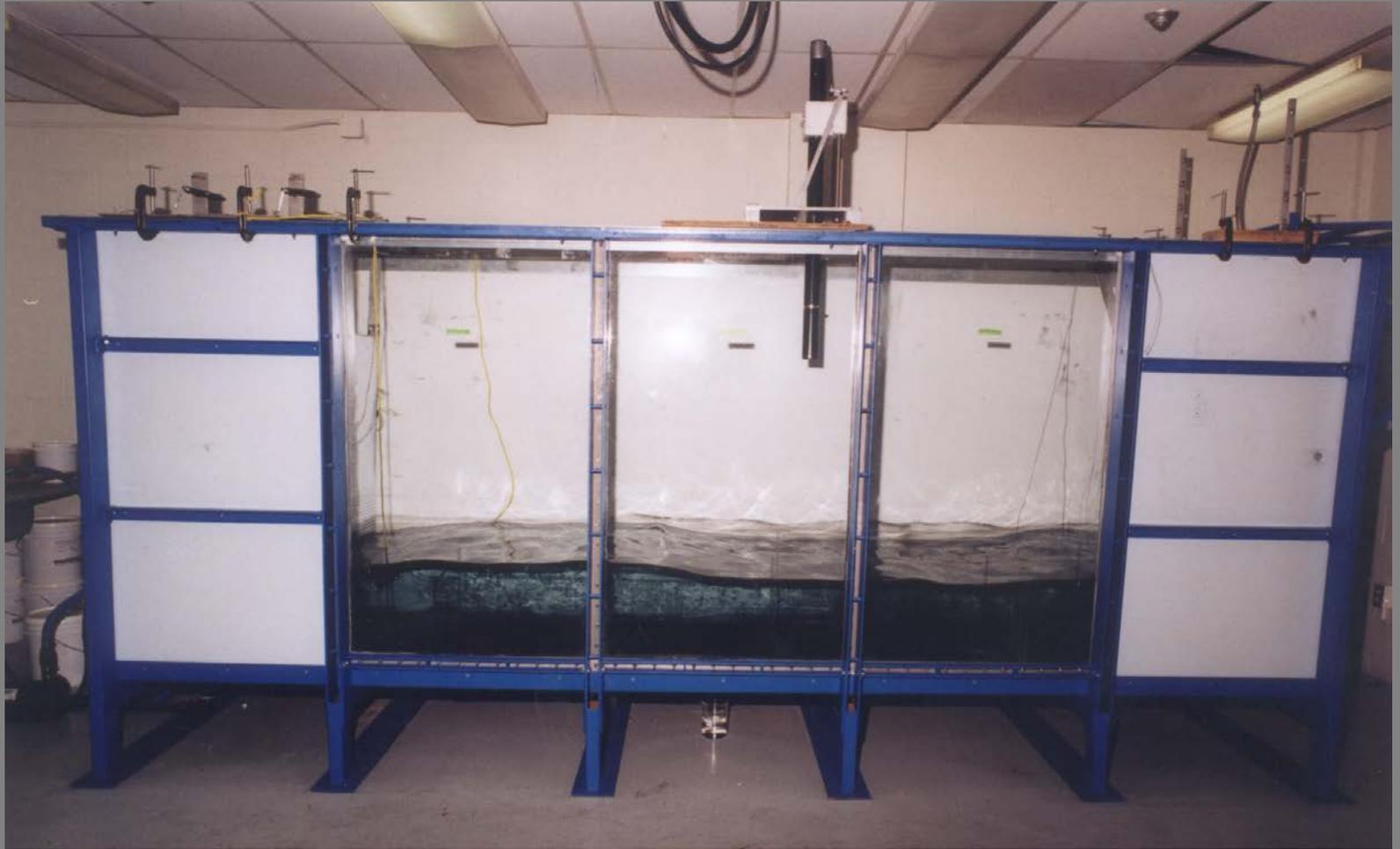
Elemental Analysis

	Nitrogen (%)	Organic Carbon (%)	Sulfur (%)
Average Bed Tailings	0.01	0.17	3.16
Averaged Collected Tailings	0.8	7.47	1.39

Wave Tank Assembly



Photograph

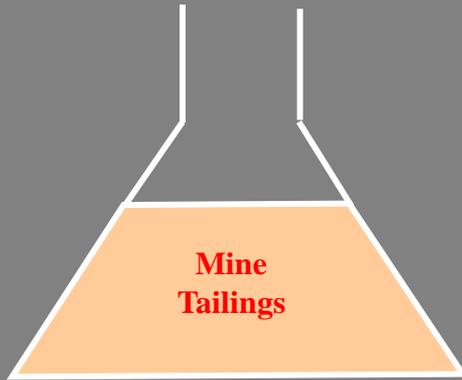




Tank settings for resuspension experiments

Parameters	Values
Cylinder diameter	0.20 m
Wave height (H)	0.07 m
Wave frequency	0.622 Hz
Water level (h)	0.35 m
H/h ratio	0.20
Wave length (L)	2.70 m
Celerity (C)	1.76 m/s

Oxidation rate from shake flask



Shake flask

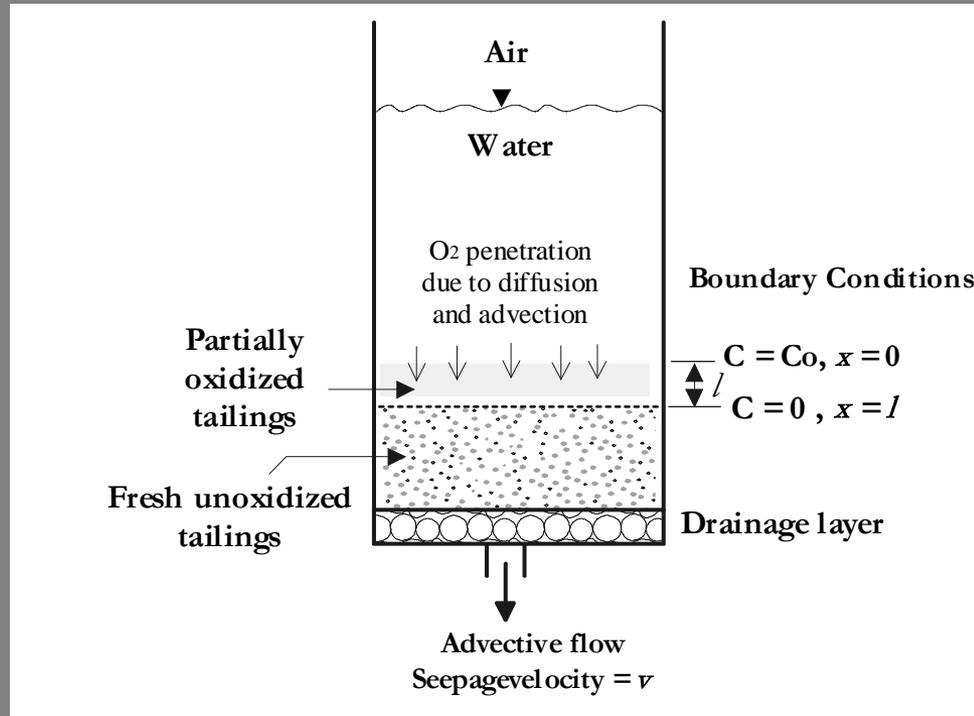
$$\frac{dC_{\text{SO}_4^{2-}}}{dt} = -\frac{2}{3.75} \frac{dC_{\text{O}_2}}{dt}$$

$$47 \text{ mg SO}_4^{2-} \text{ L}^{-1} \text{ day}^{-1}$$

$$220 \times 10^{-9} \text{ mole SO}_4^{2-} \text{ kg}^{-1} \text{ s}^{-1}$$

$$60.73 \times 10^{-10} \text{ mole O}_2 \text{ m}^{-2} \text{ s}^{-1}$$

Diffusion model



- Completely mixed water
- No resuspension
- Advection

$$\frac{\partial C}{\partial t} = D_1^* \frac{\partial^2 C}{\partial x^2} - v \frac{\partial C}{\partial x} - K_1^* C$$

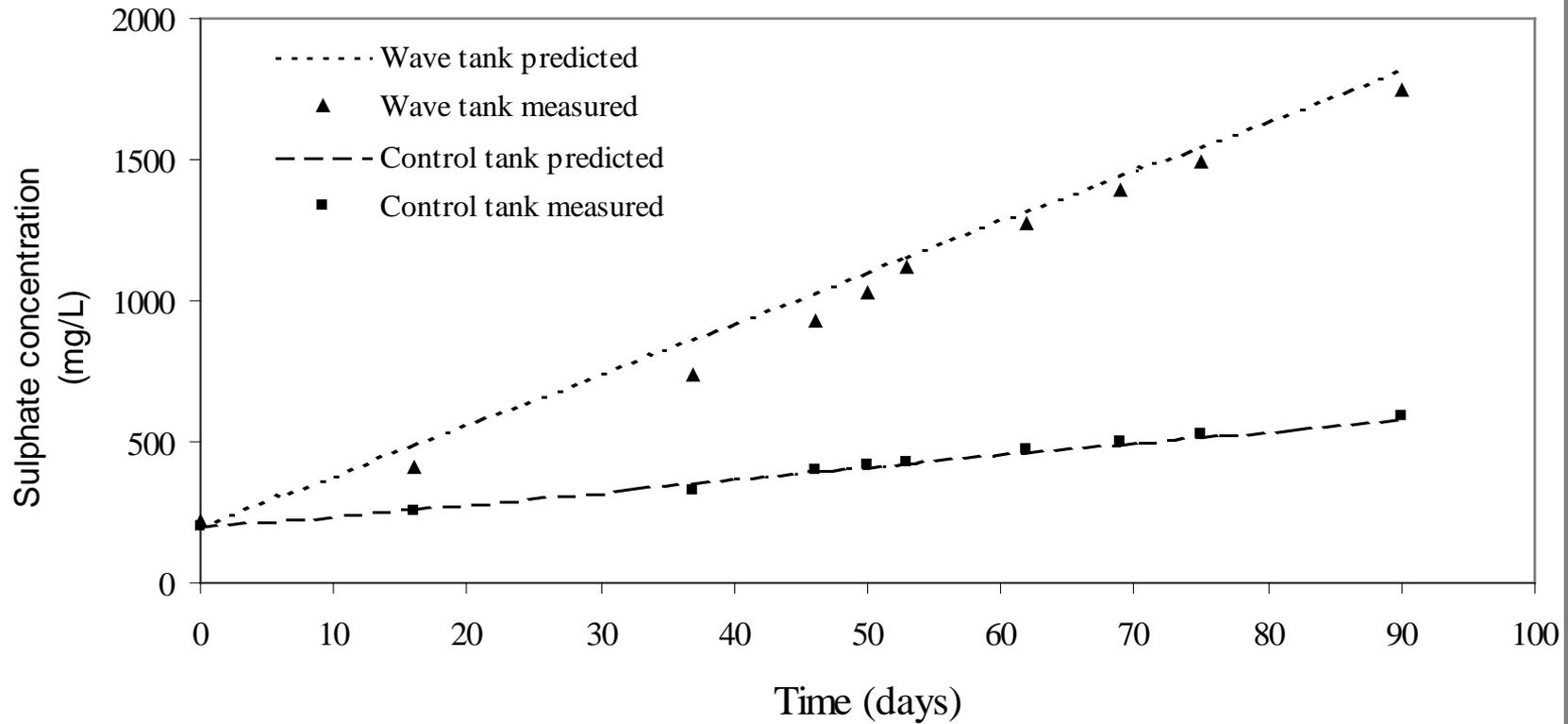
$$flux = -\frac{v}{2} C_0 \left(1 - \sqrt{1 + \frac{4K_1^* D_1^*}{v^2}} \right)$$

Model representing experimental tanks

Sulphate production rate from the wave tank = Background sulphate concentration + Sulphate produced due to resuspension of tailings + Sulphate produced due to diffusion of oxygen into submerged tailings

$$\left(\frac{mgSO_4^{-2}}{L}\right) = C_b + \frac{10 \times s \times a_0}{h \times t_d^\alpha} T_t \left(\frac{\tau - \tau_c}{\tau_c}\right)^\beta + \frac{1.3824 \times 10^8 \times T_t \times C_0 \sqrt{D^* K^*}}{h}$$

Sulphate concentration

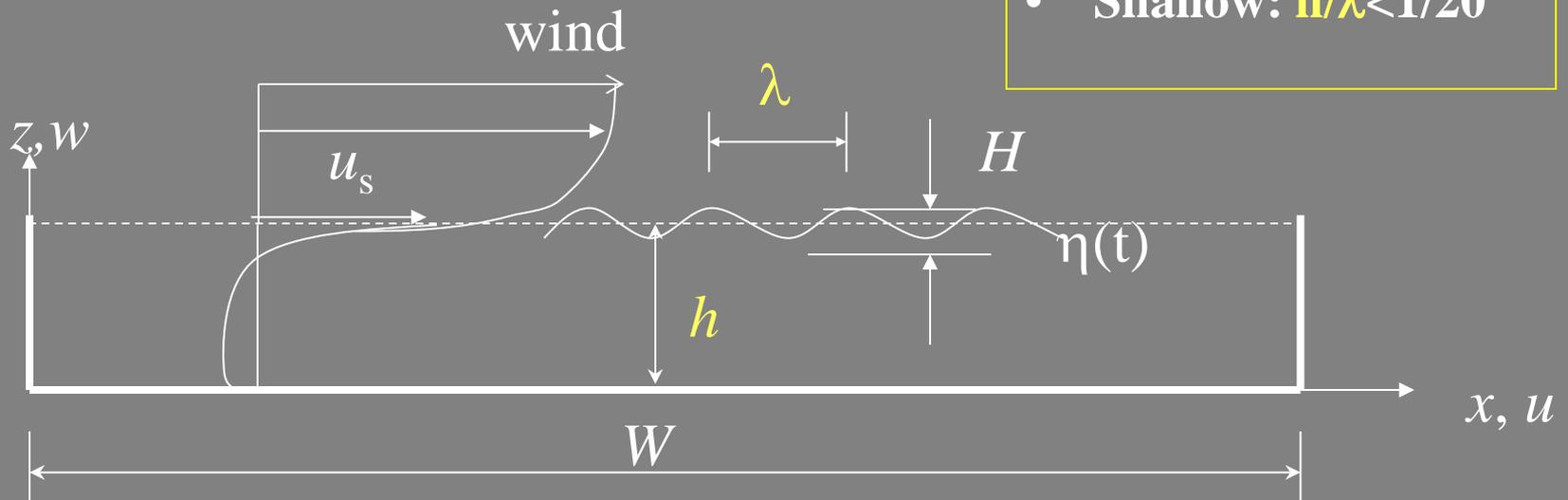


Study of surface **shear** and **waves** induced countercurrent flow

- Experimental Study
- Mathematical modeling

Classification of waves

- Deep: $h/\lambda > 1/2$
- Intermediate: $1/20 < h/\lambda < 1/2$
- Shallow: $h/\lambda < 1/20$



Experimental study



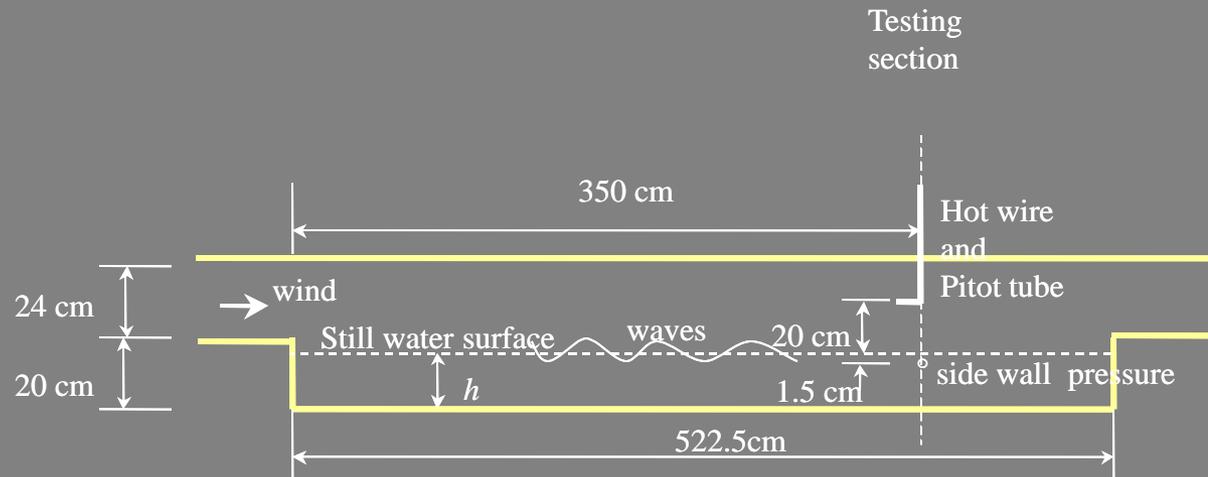
Controlled
wind speed,
water depth,

Closed-circuit wind-wave tunnel in Boundary Layer Wind Tunnel Laboratory, the University of Western Ontario, London, Ontario, Canada

Schematic of wind-wave tunnel

Measurements:

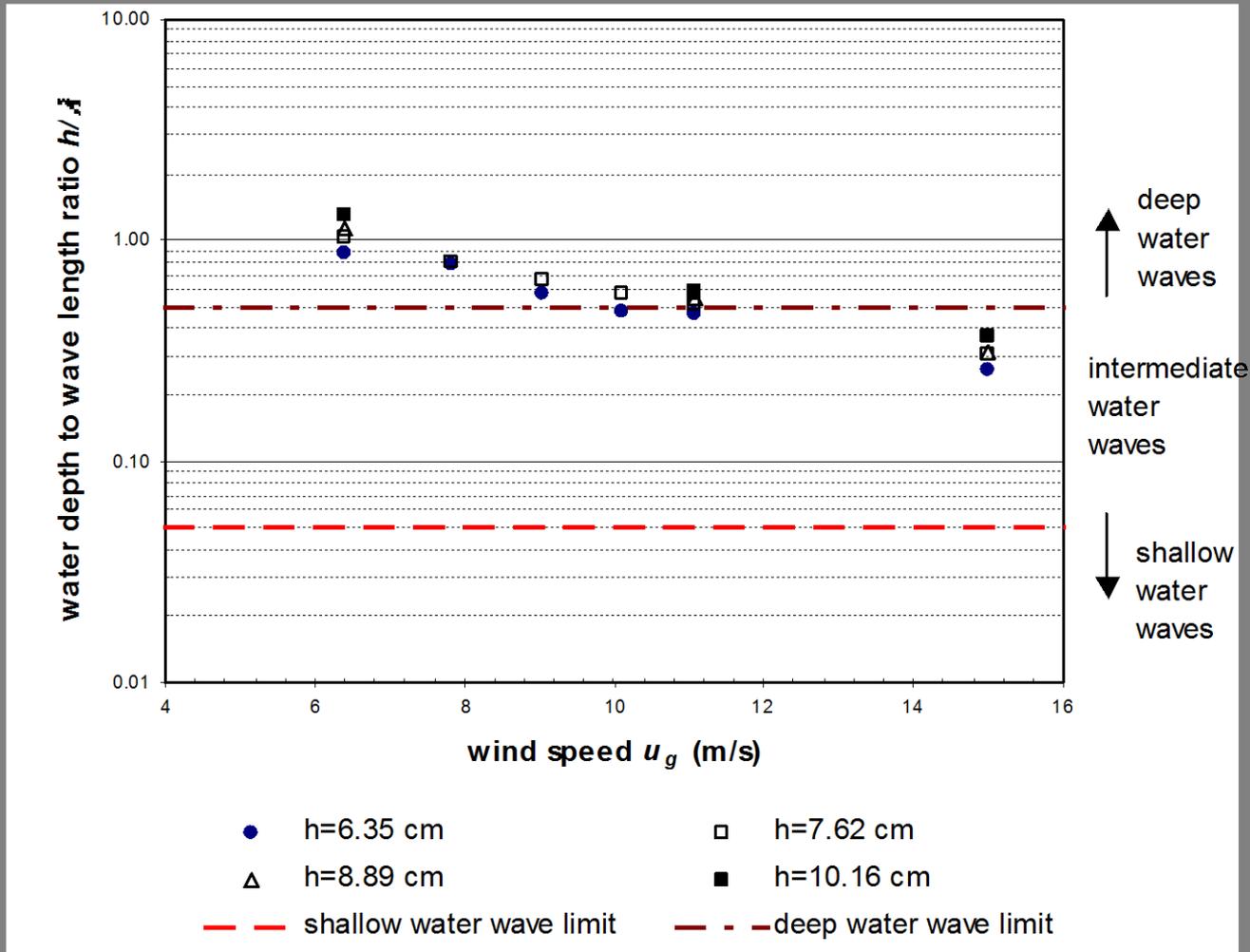
- Wind speed
- Wave height
- Pressure
- Velocity of water



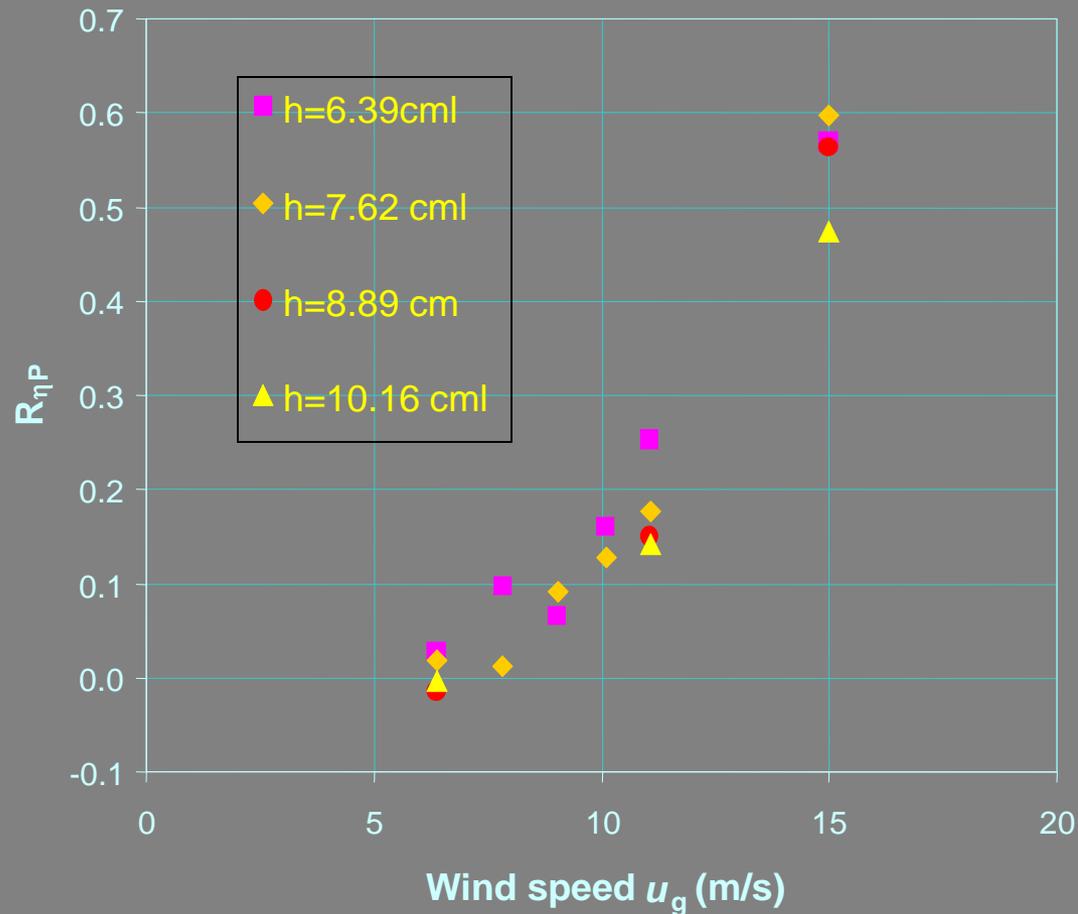
Objective

- Describe the impact of surface wind-waves on the flow structure;
- Develop a simple mathematical model to describe the flow motions.

Classification of measured waves



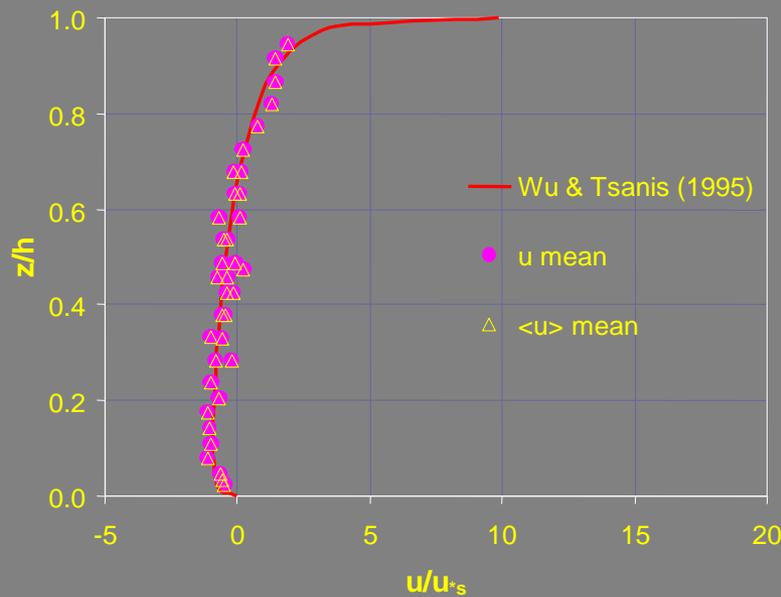
Water surface and bottom pressure correlation versus wind speed



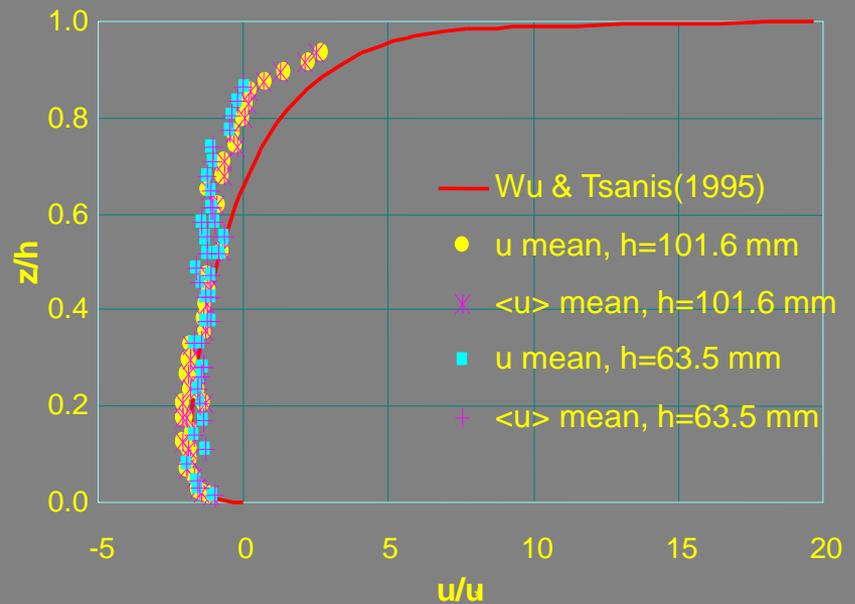


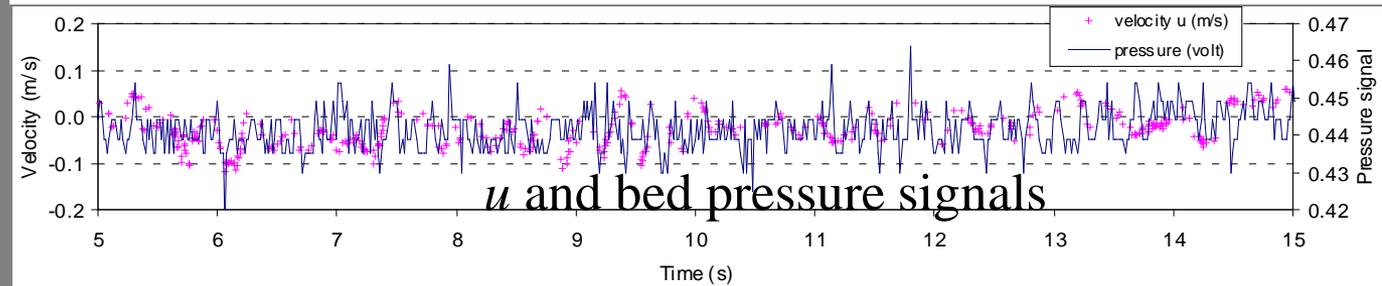
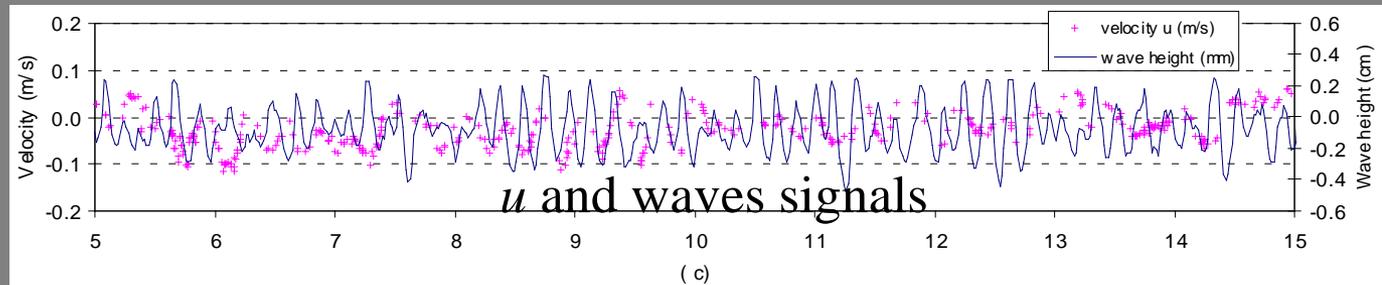
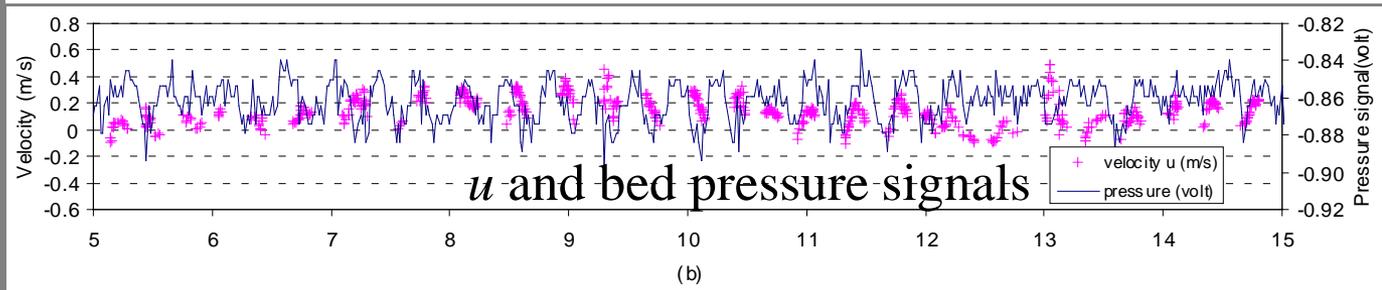
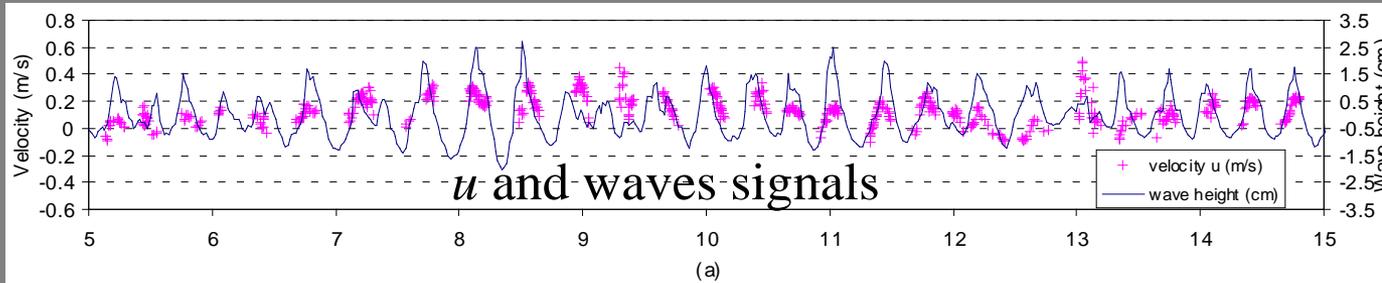
Comparison btwn measured and existed model predicted mean velocity \bar{u} in vertical plane

Deep water-wave



Intermediate water-wave





Intermediate water waves:
Periodic flow motion

Deep water waves:
Non-periodic Flow motion

Triple Decomposition Theory

Hussain and Reynolds (1970)

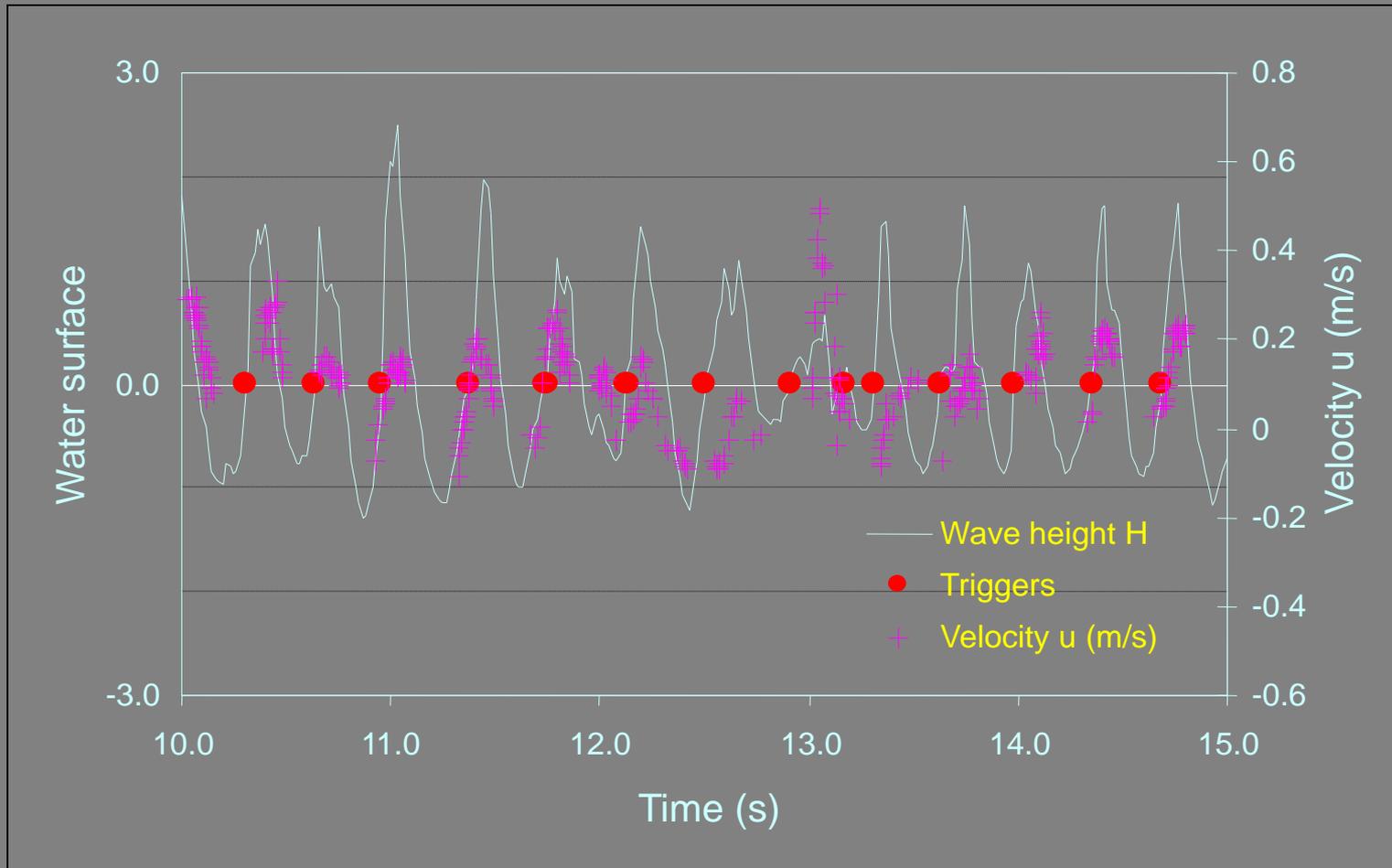
$$f(x, t) = \bar{f}(x) + f_c(x, t) + f'_r(x, t) = \langle f(x, t) \rangle + f'_r(x, t)$$

$$\bar{f}(x) = \lim_{T_0 \rightarrow \infty} \frac{1}{T_0} \sum_{n=0}^{n=N} \int f(x, t) dt$$

$$\langle f(x, t) \rangle = \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{n=0}^{n=N} f(x, t + nT)$$

$$f_c = \langle f \rangle - \bar{f}$$

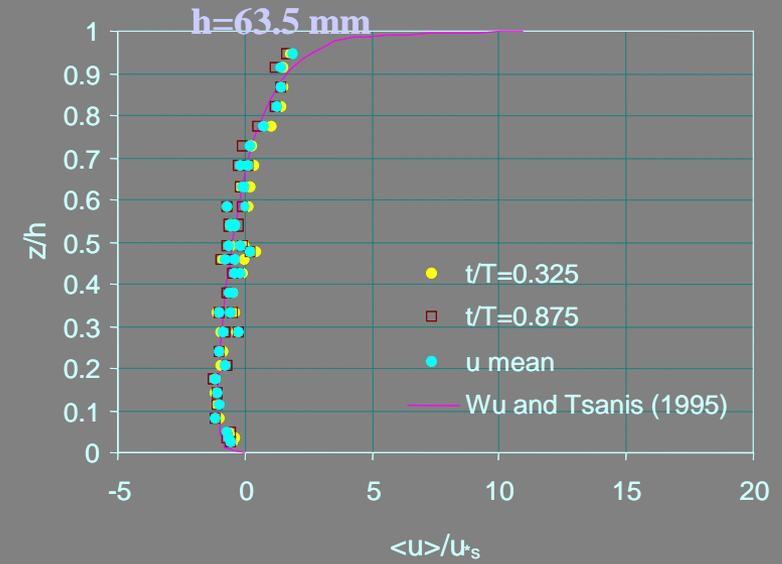
Wave, velocity signals and selected triggers for a typical experimental record



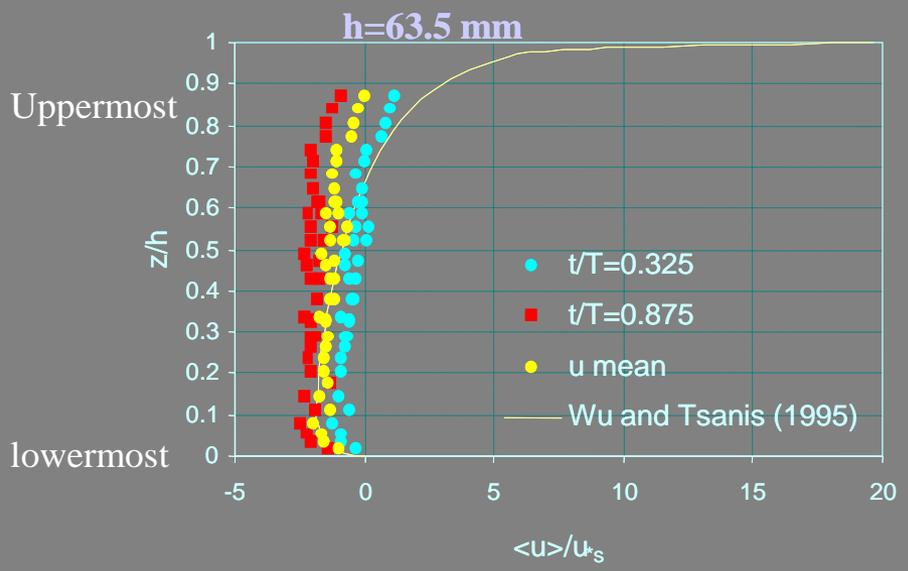


Phase averaged velocity
in vertical plane
during acceleration ($t/T=0.325$) and
deceleration ($t/T=0.875$):

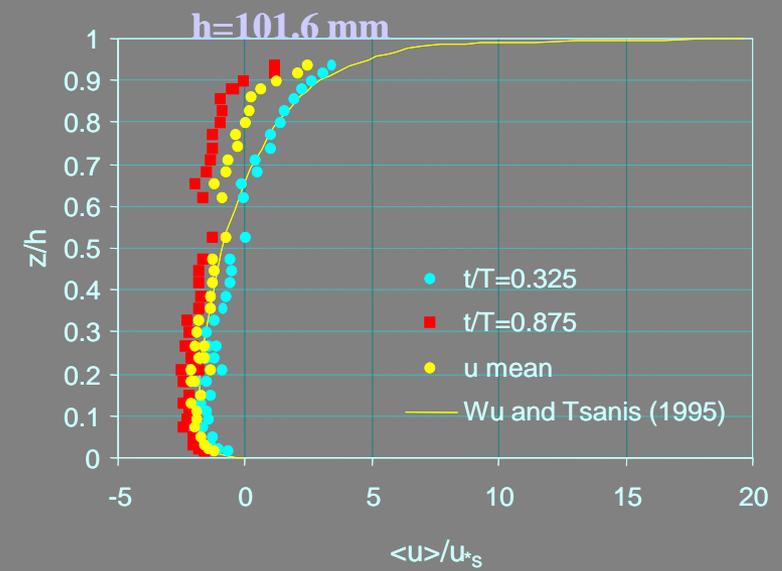
(a) Deep water waves



(b) Intermediate water waves

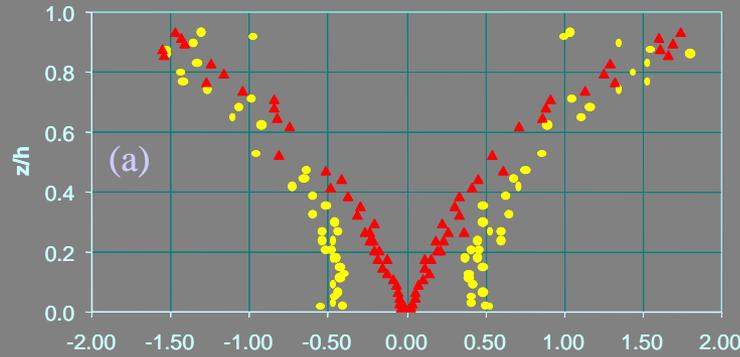


(c) Intermediate water waves

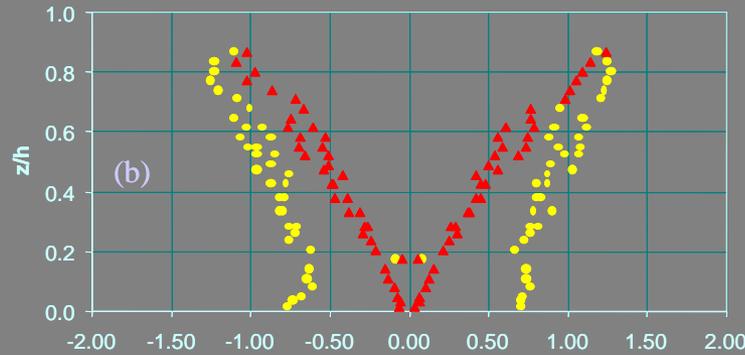




intermediate
water-wave

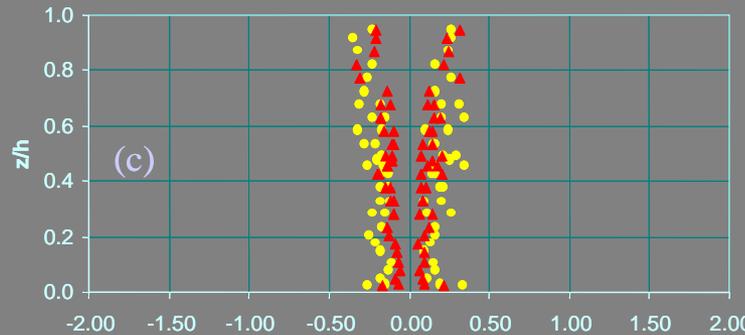


Max. & min.
coherent velocity
components in
vertical plane.



Intermediate:
Significant

deep
water-wave

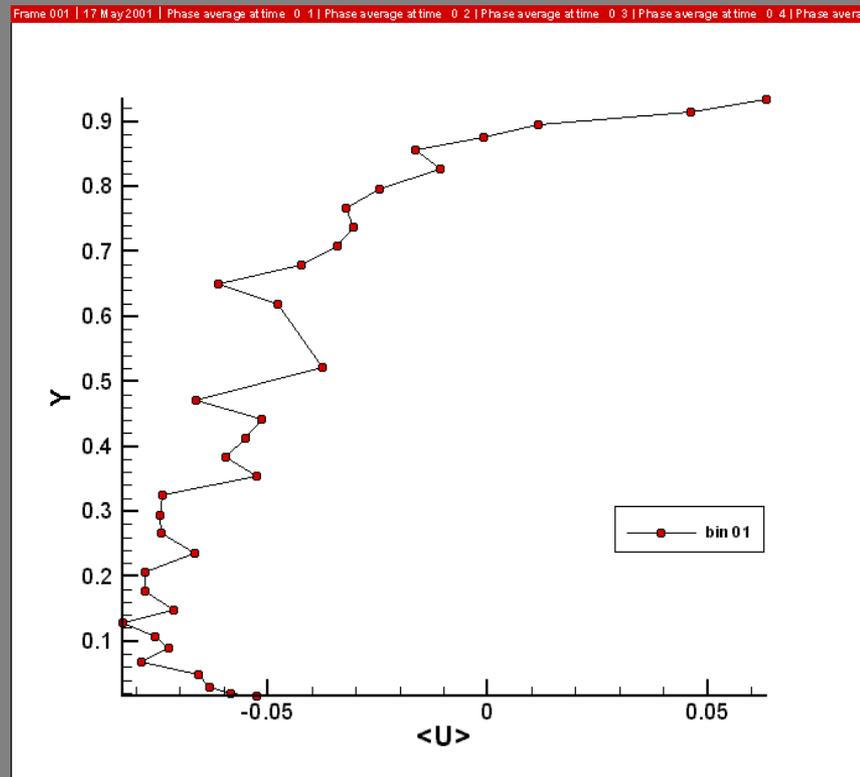


Deep:
negligible

● U_c max. $h=63.5$ mm ● U_c min. $h=63.5$ mm
▲ V_c max. $h=63.5$ mm ▲ V_c min. $h=63.5$ mm

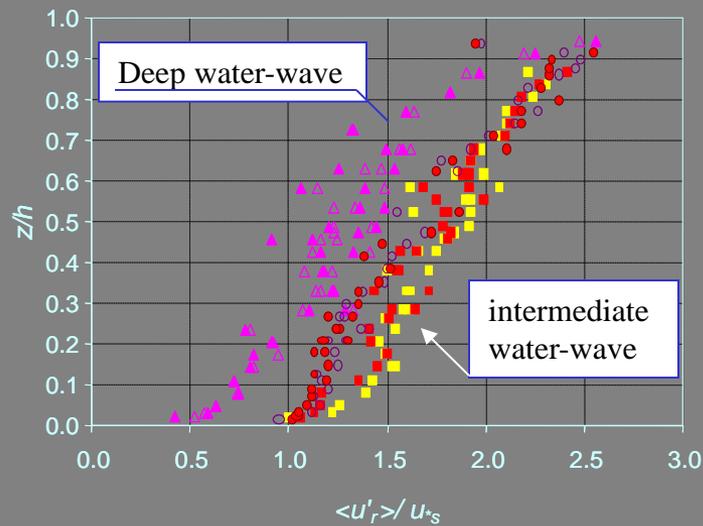
$u_c \max / u_s$

Phase-averaged velocity $\langle u \rangle$ varies in a wave period (intermediate water wave conditions)

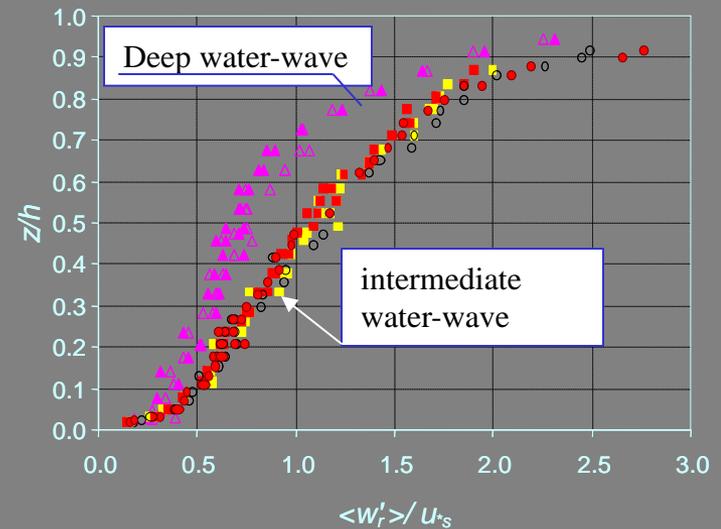


Distribution of random fluctuating components in vertical plane

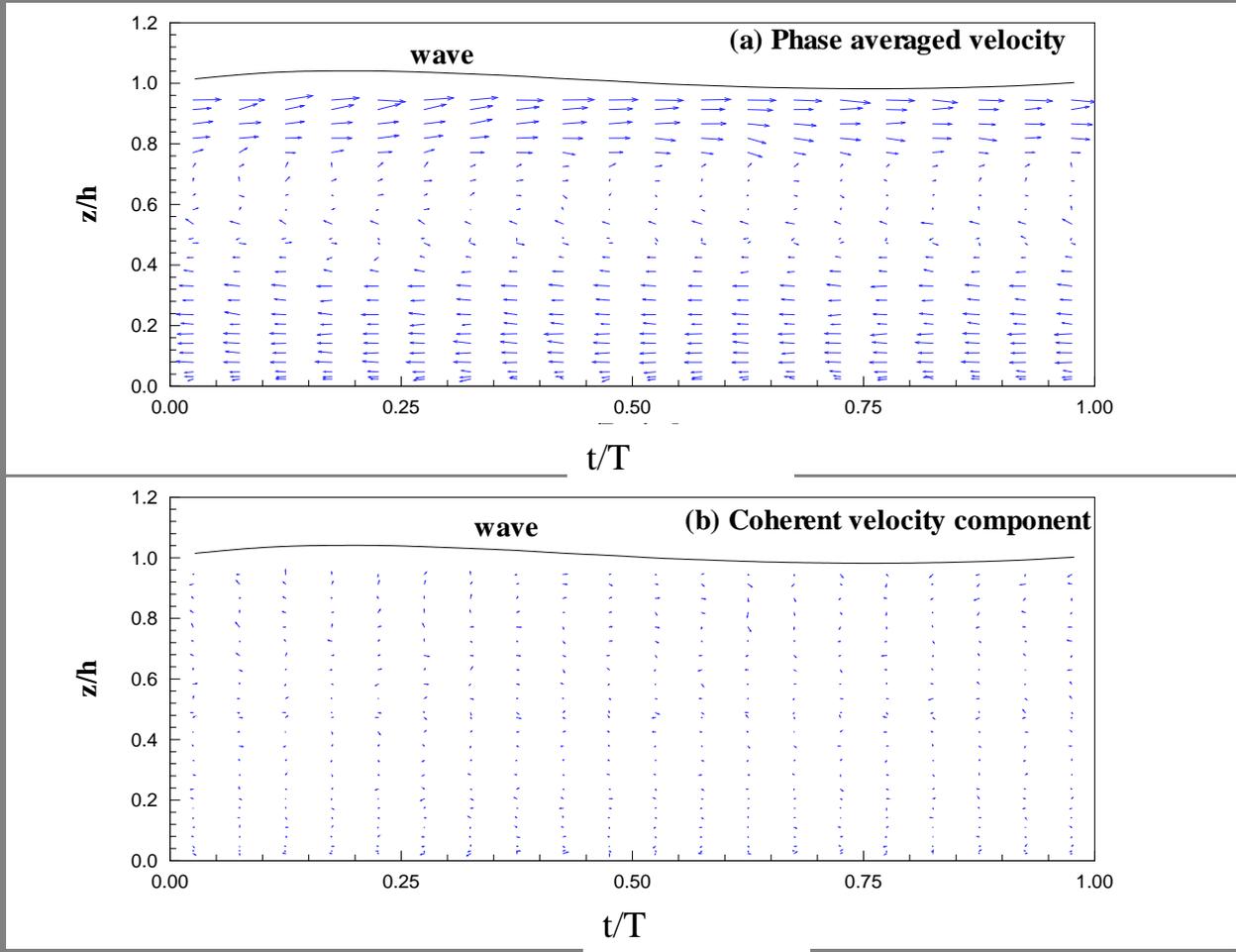
(a) Horizontal components



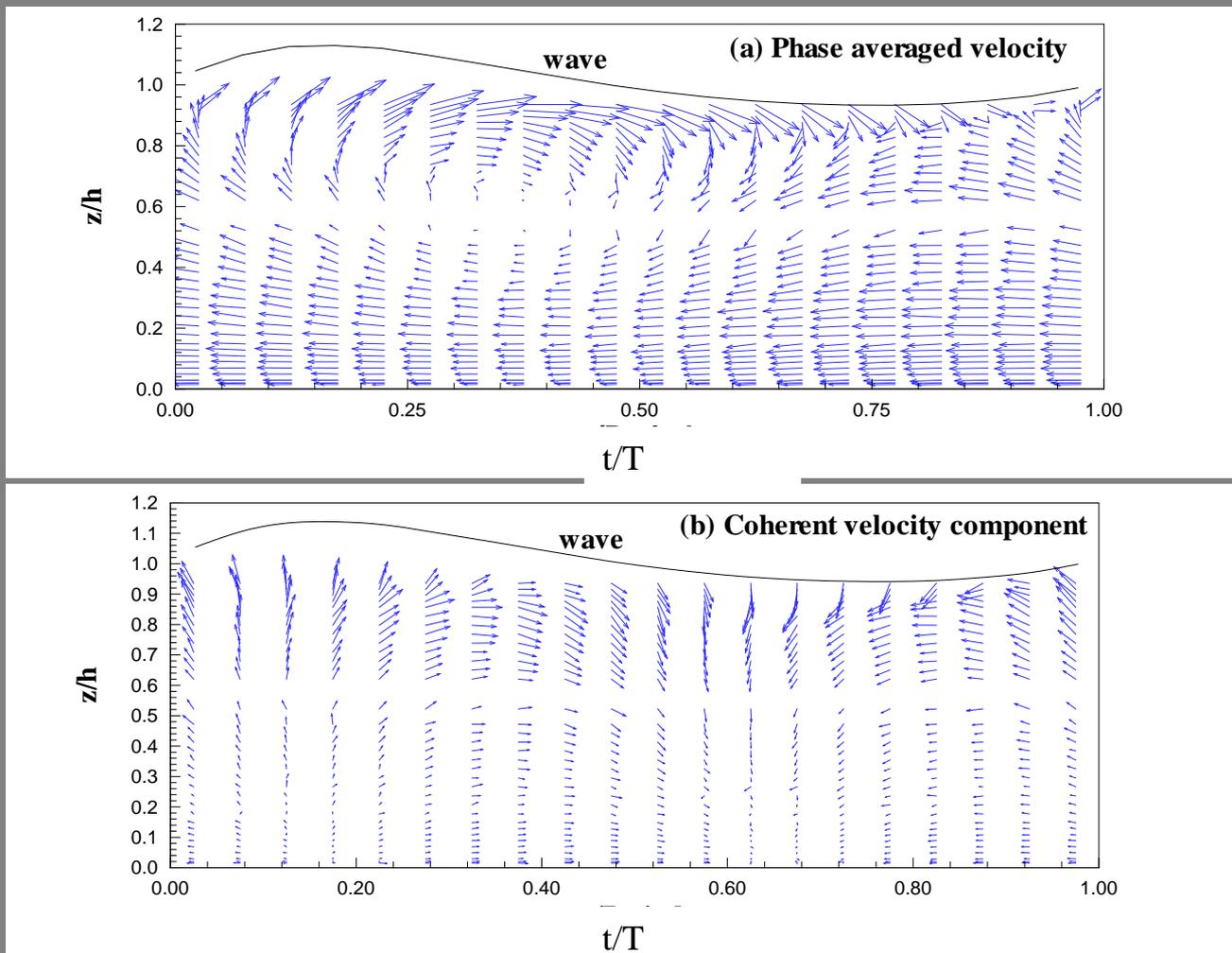
(b) Vertical components



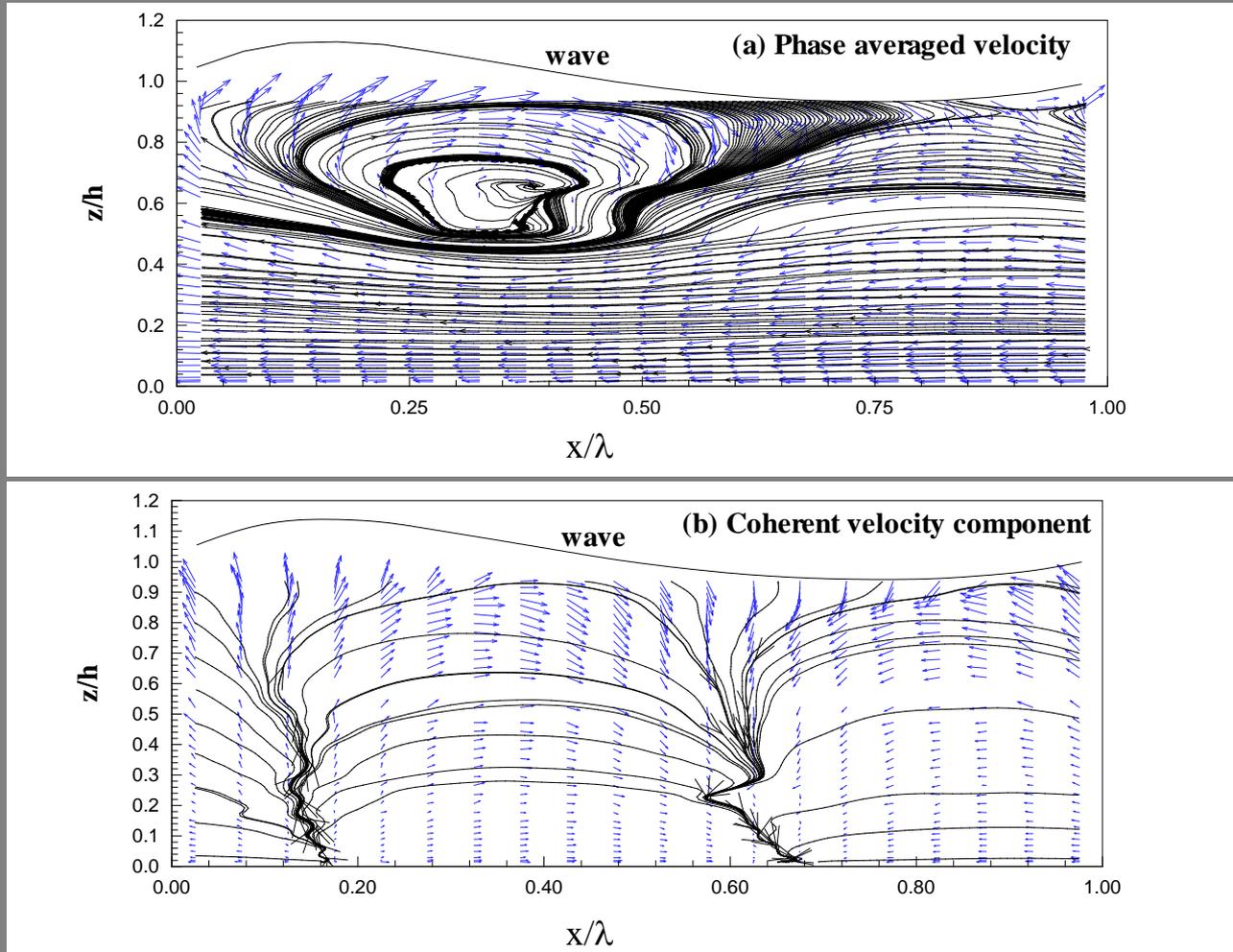
Vector plot in a period for $u_g=6.39$ m/s and $h=63.5$ mm
(deep water wave conditions)



Vector plot in a period for $u_g=15$ m/s and $h=101.6$ mm
(intermediate water wave condition)



Vector and streamline plot in one wavelength for wind speed $u_g=15$ m/s and water depth $h=101.6$ mm (intermediate water wave condition)





Mathematical modeling

- Time-averaged components
- Coherent components

$$\langle u(z, t) \rangle = \bar{u}(z) + u_c(z, t)$$

$$\langle w(z, t) \rangle = w_c(z, t)$$

Modeling of time-averaged component

Governing equations

$$\frac{\partial \bar{w}}{\partial z} = 0$$

$$-\frac{1}{\rho} \frac{\partial p}{\partial x} + \frac{\partial}{\partial z} \left(\nu_{eff} \frac{\partial \bar{u}}{\partial z} \right) = 0$$

$$-\frac{1}{\rho} \frac{\partial p}{\partial z} = 0$$

Where: $\nu_{eff} = \nu + \nu_t$

Boundary conditions

$$z=h: \quad u=u_s \quad \text{or} \quad \tau = \rho u_{*s}^2$$

$$z=0: \quad u=0$$

Constrain for countercurrent flow

$$\int_0^h \bar{u} dz = 0$$

Modification of eddy viscosity

Tsanis suggested eddy viscosity (1989):

$$\nu_t = \frac{\lambda u_{*s}}{h} (z + z_b)(z_s + h - z)$$

Proposed eddy viscosity

$$\nu_t = \frac{\lambda u_{*s}}{h} (z + z_b)(z_s + h - z) \left(1 + a \frac{z}{h} \right)$$

Proposed Model of *time-averaged* velocity

$$\frac{\bar{u}}{u_{*s}} = A \ln\left(1 + \frac{z}{z_b}\right) + B \ln\left(1 - \frac{z}{z_s + h}\right) + C \ln\left(1 + a \frac{z}{h}\right)$$

$$A = \frac{(1+a) \ln(1+a) - az_{sh} \ln\left(1 + \frac{1}{z_{sh}}\right)}{D}$$

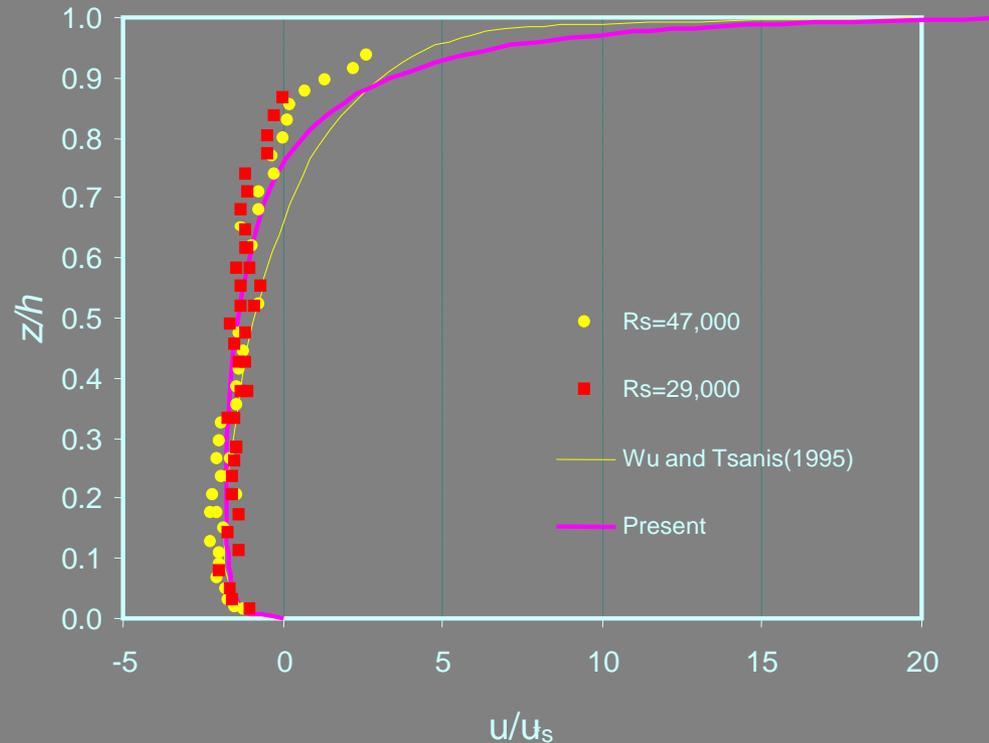
$$B = \frac{(1+a) \ln(1+a) - a(1+z_{bh}) \ln\left(1 + \frac{1}{z_{bh}}\right)}{D}$$

$$C = \frac{a(1+z_{bh}) \ln\left(1 + \frac{z}{z_{bh}}\right) - az_{sh} \ln\left(1 + \frac{1}{z_{sh}}\right)}{D}$$

$$D = \lambda \left\{ a \left[1 + a(1+z_{sh}) \right] (1+z_{bh})^2 \ln\left(1 + \frac{1}{z_{bh}}\right) + az_{sh}^2 (1-z_{bh}) \ln\left(1 + \frac{1}{z_{sh}}\right) - (1+z_{bh} + z_{sh})(1+a)^2 \ln(1+a) \right\}$$

Comparison btwn proposed-model predicted and experimental *time-averaged* u components

$\lambda=1.0$, $z_{bh}=0.00014$, $z_{sh}=0.01$ and $a=-0.9$



Modeling of *coherent* components

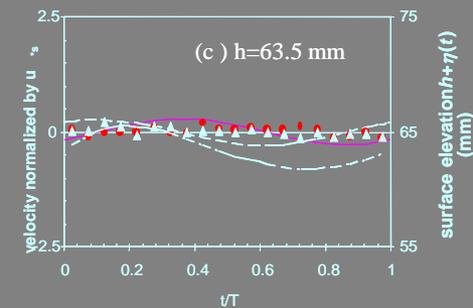
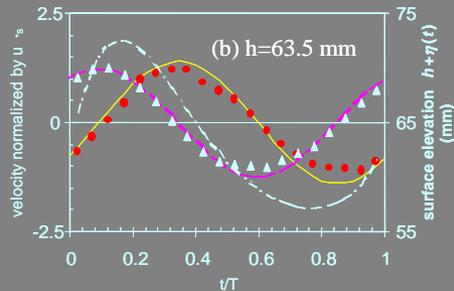
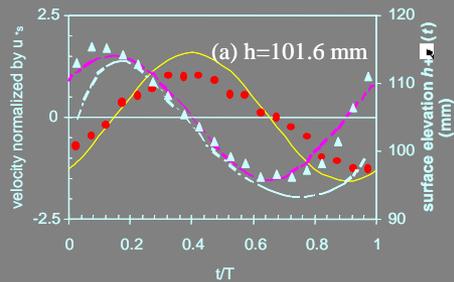
The water particle orbital velocity in a wave can be obtained from the potential flow assumption (i.e. Sorensen, 1993):

$$u(x, z, t) = \frac{\pi H}{T} \frac{\cosh(kz)}{\sinh(kh)} \cos(kx - \sigma t)$$

$$w(x, z, t) = \frac{\pi H}{T} \frac{\sinh(kz)}{\sinh(kh)} \sin(kx - \sigma t)$$

Comparison of model predicted and experimental *coherent* components

Uppermost point

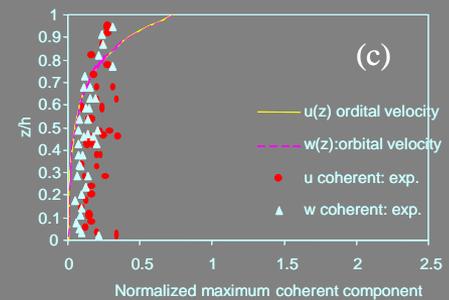
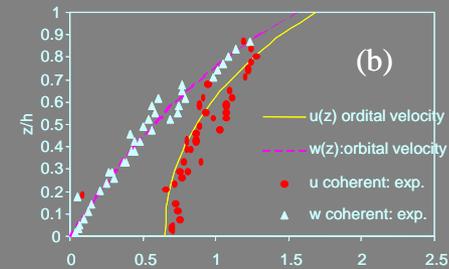
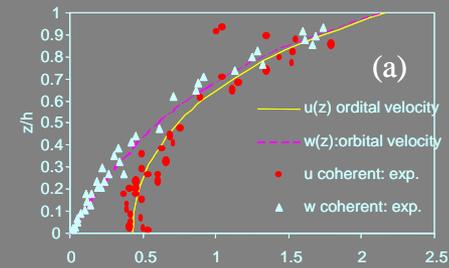


— u orbital velocity - - - w orbital velocity ● u coherent
 ▲ w coherent ····· surface elevation

Intermediate water wave

Deep-water wave

Vertical distribution



Normalized maximum coherent component

Intermediate water wave

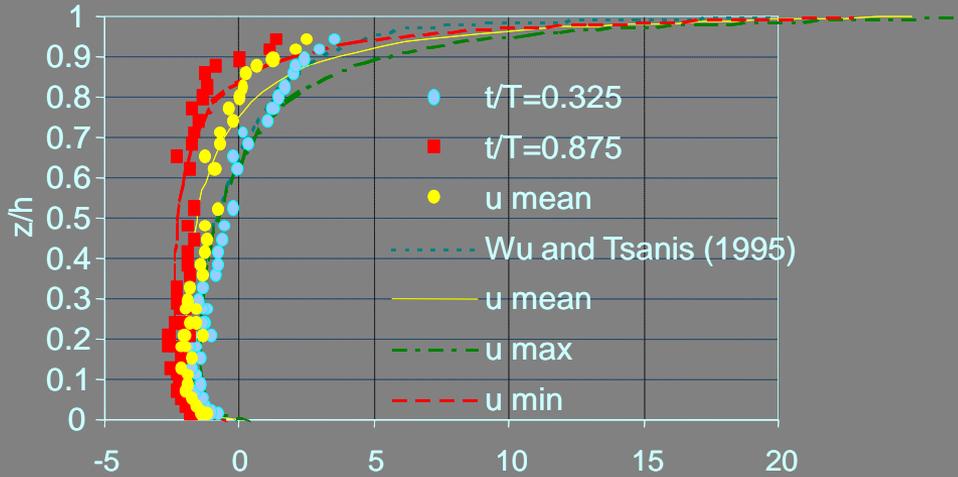
Deep-water wave

Proposed general model for wind-induced countercurrent flow

$$\left\langle \frac{u(x, z, t)}{u_{*s}} \right\rangle = \underbrace{A \ln \left[1 + \frac{z}{z_b} \right] + B \ln \left[1 - \frac{z}{z_s + h} \right]}_{\substack{\text{due to surface shear} \\ \text{time averaged term}}} + \underbrace{C \ln \left(1 + a \frac{z}{h} \right)}_{\text{due to waves}} + \underbrace{\frac{\pi H}{Tu_{*s}} \left[\frac{\cosh(kz)}{\sinh(kh)} \right] \cos(kx - \sigma t)}_{\text{coherent velocity term}} \quad 0 \leq z \leq h$$

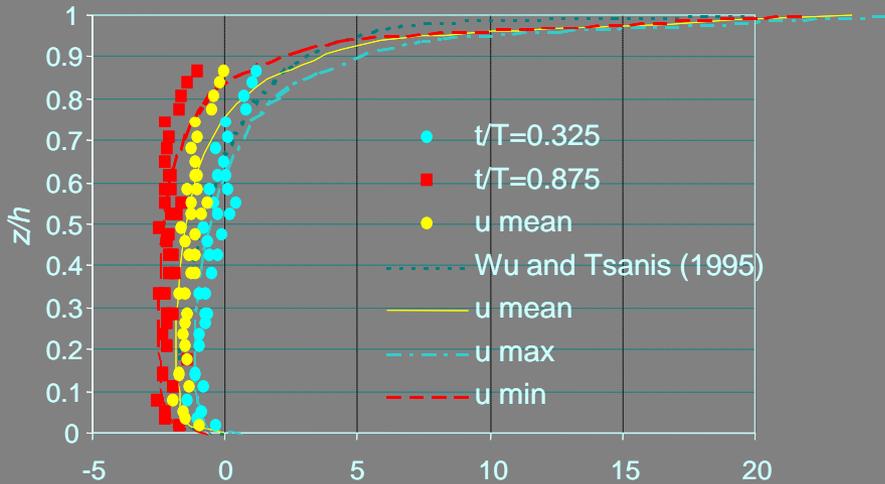
$$\left\langle \frac{w(x, z, t)}{u_{*z}} \right\rangle = \underbrace{\frac{\pi H}{Tu_{*s}} \left[\frac{\sinh(kz)}{\sinh(kh)} \right] \sin(kx - \sigma t)}_{\text{coherent velocity term}} \quad 0 \leq z \leq h$$

(a) Intermediate water wave
 $h/\lambda=0.369$, $h=101.6$ mm

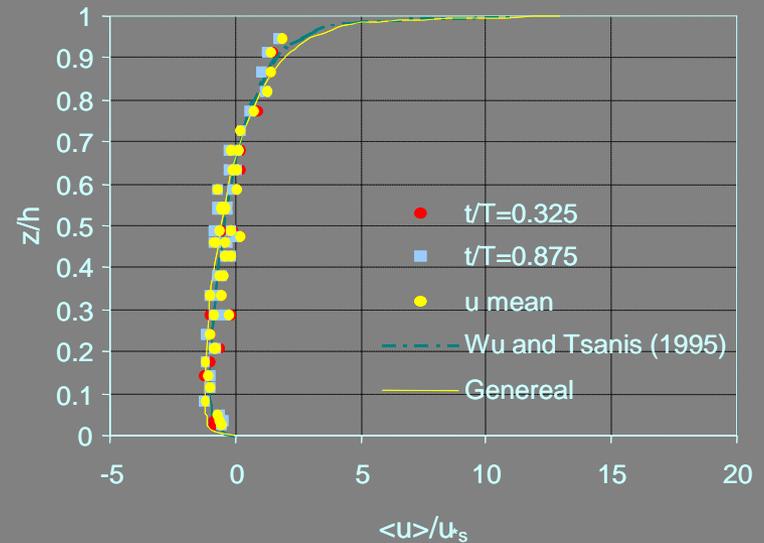


Comparison of
 experimental and
 model predicted
phase-averaged
 velocity $\langle u \rangle$

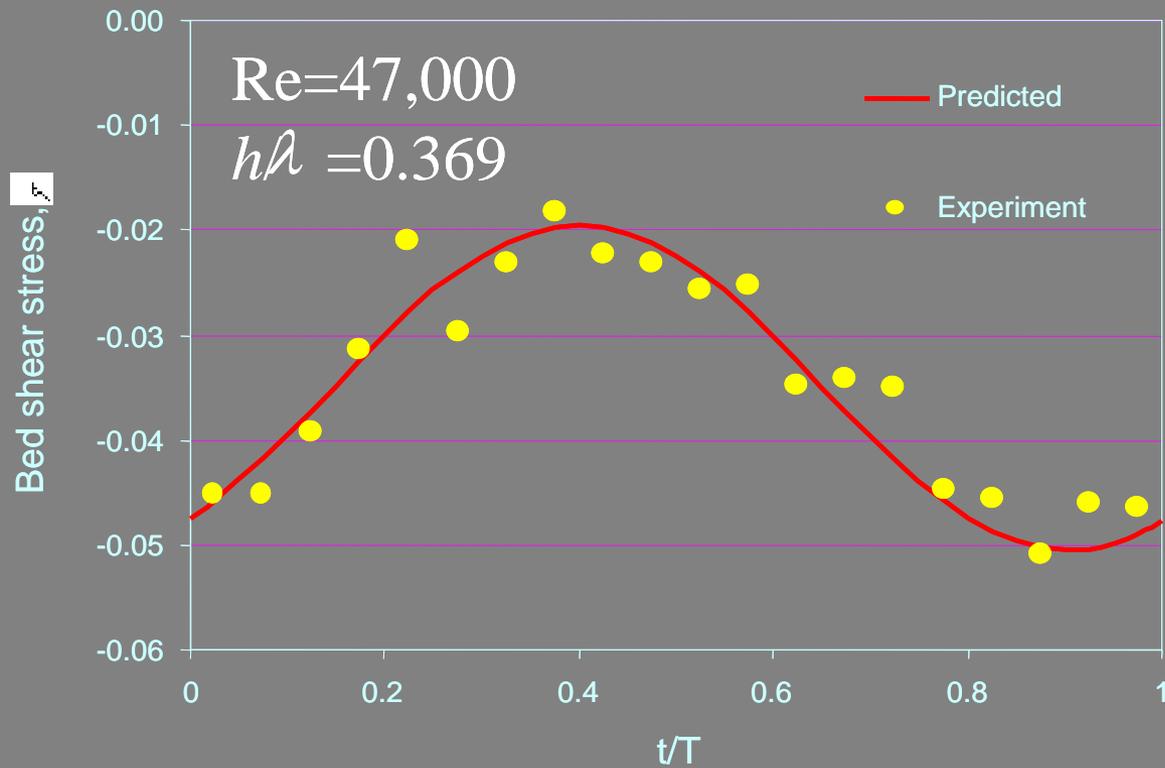
(b) intermediate water wave
 $h/\lambda=0.258$, $h=63.5$ mm



(c) Deep water wave
 $h/\lambda=0.866$, $h=63.5$ mm



Proposed-model predicted and experimental bed shear stress



Summary and Conclusions

- The influence of wind-generated water-waves on the flow field is significant under intermediate water-wave conditions, in both the time-averaged and coherent structures of the flow.
- The coherent velocity is closely correlated with surface waves and satisfies linear wave theory, which varies periodically at the frequency of surface waves.
- An organized vortex structure is found in the upper parts of water under intermediate water-waves conditions, which rotates clockwise and travels at the speed of surface waves in the direction of the wind.

Summary and Conclusions (continue)

- The model developed to describe the velocity components is seen to be in excellent agreement with the experimental data and can recover the results of Tsanis (1989) and Wu and Tsanis (1995) for deep-water wave condition.
- The bed shear stress is found to vary periodically with the surface wave frequency under intermediate water waves. Thus, the time-averaged shear stress is not sufficient to quantify the total shear stress.